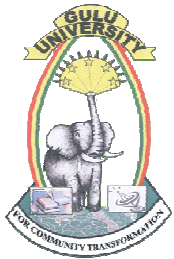


Course of General Astronomy



Gulu University

Naples FEDERICO II University



6

Temperature Equilibrium for a Planet

Nomenclature:

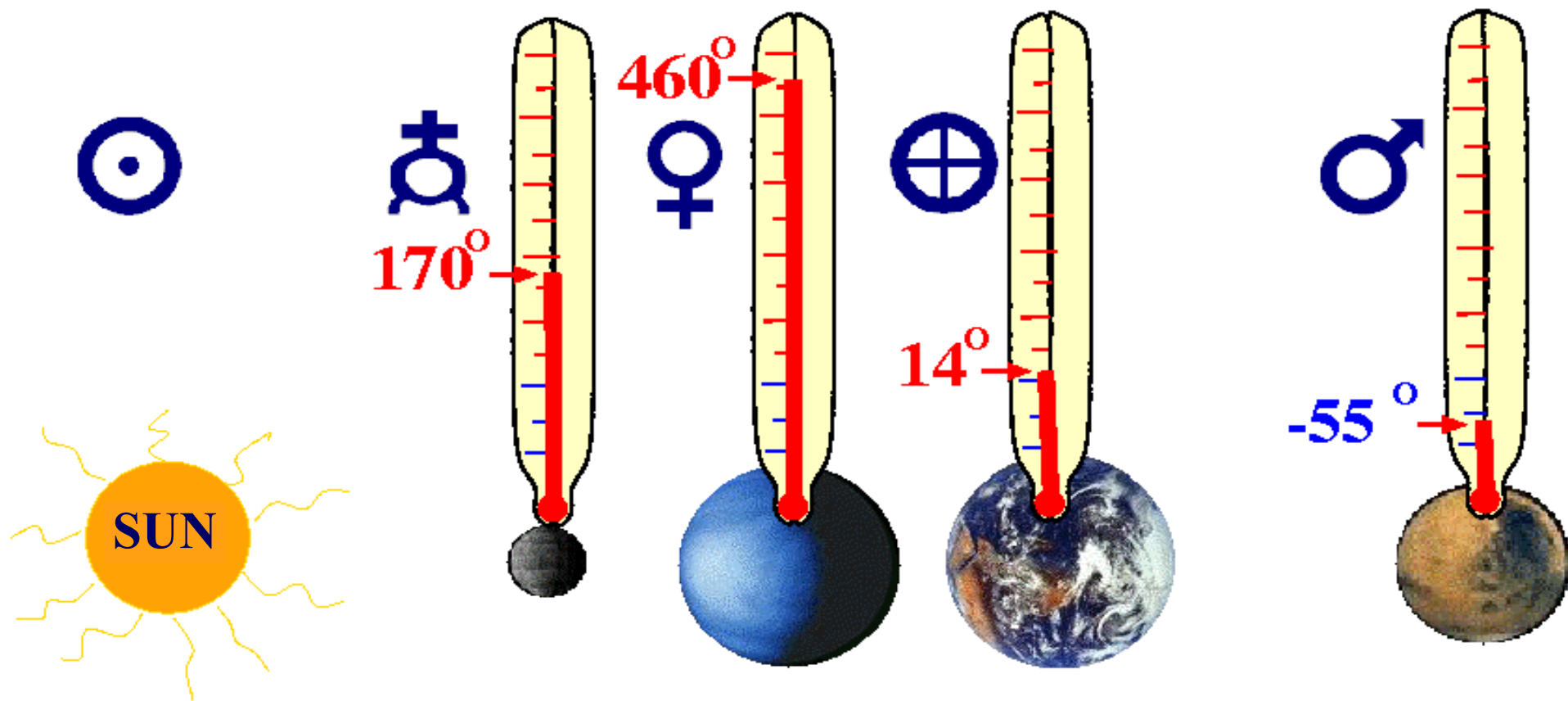


Nomenclature:



Something isn't properly working for some planet!

Mean Temperatures for Planets



Earth Mean Temperature 1860-2000:

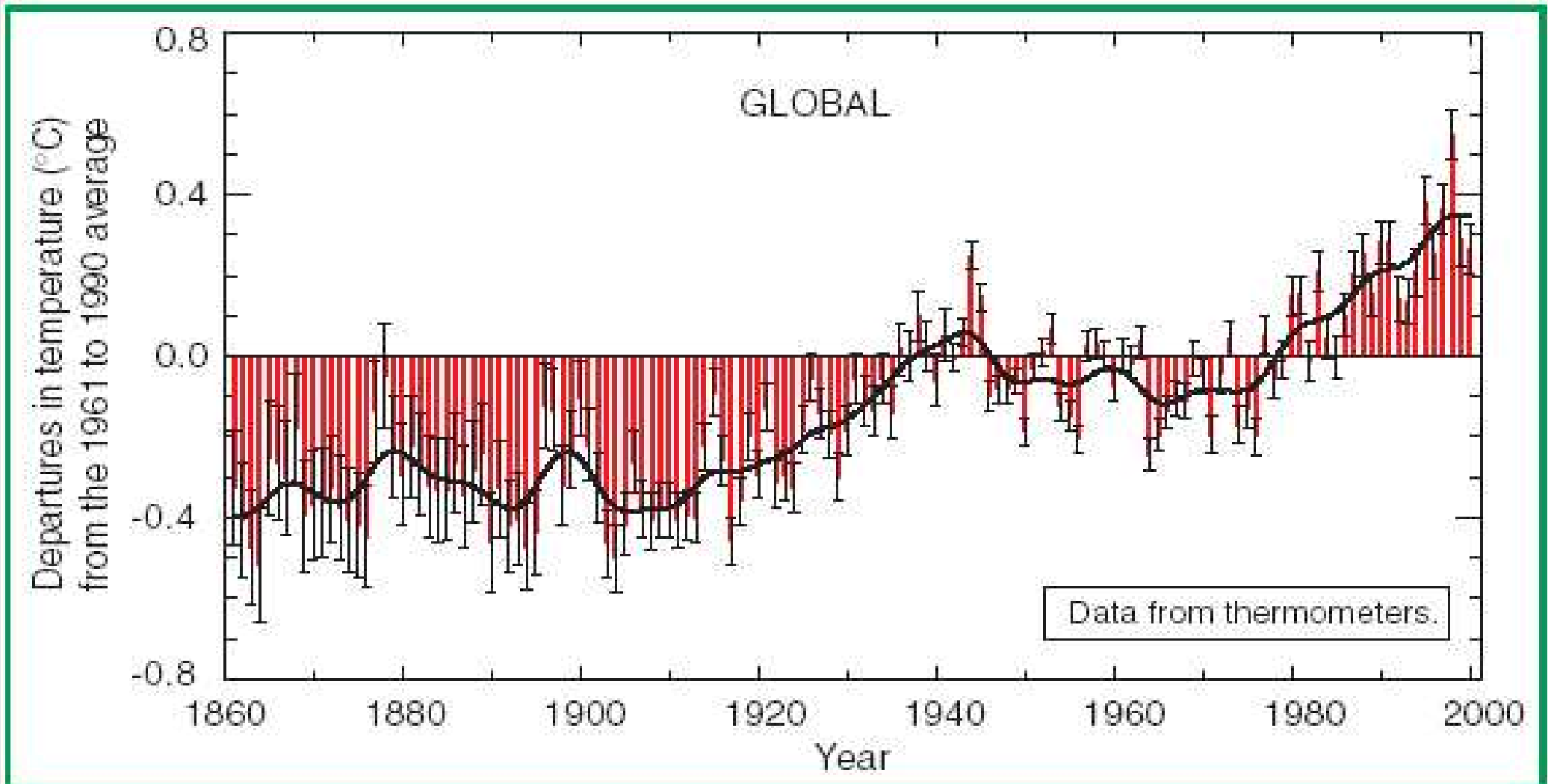


Figure 2: Combined annual land-surface air and sea surface temperature anomalies (°C) 1861 to 2000, relative to 1961 to 1990. Two standard error uncertainties are shown as bars on the annual number.

From: Intergovernmental Panel on Climate Change (IPCC) - www.ipcc.ch

Earth Mean Temperature 1000-2000:

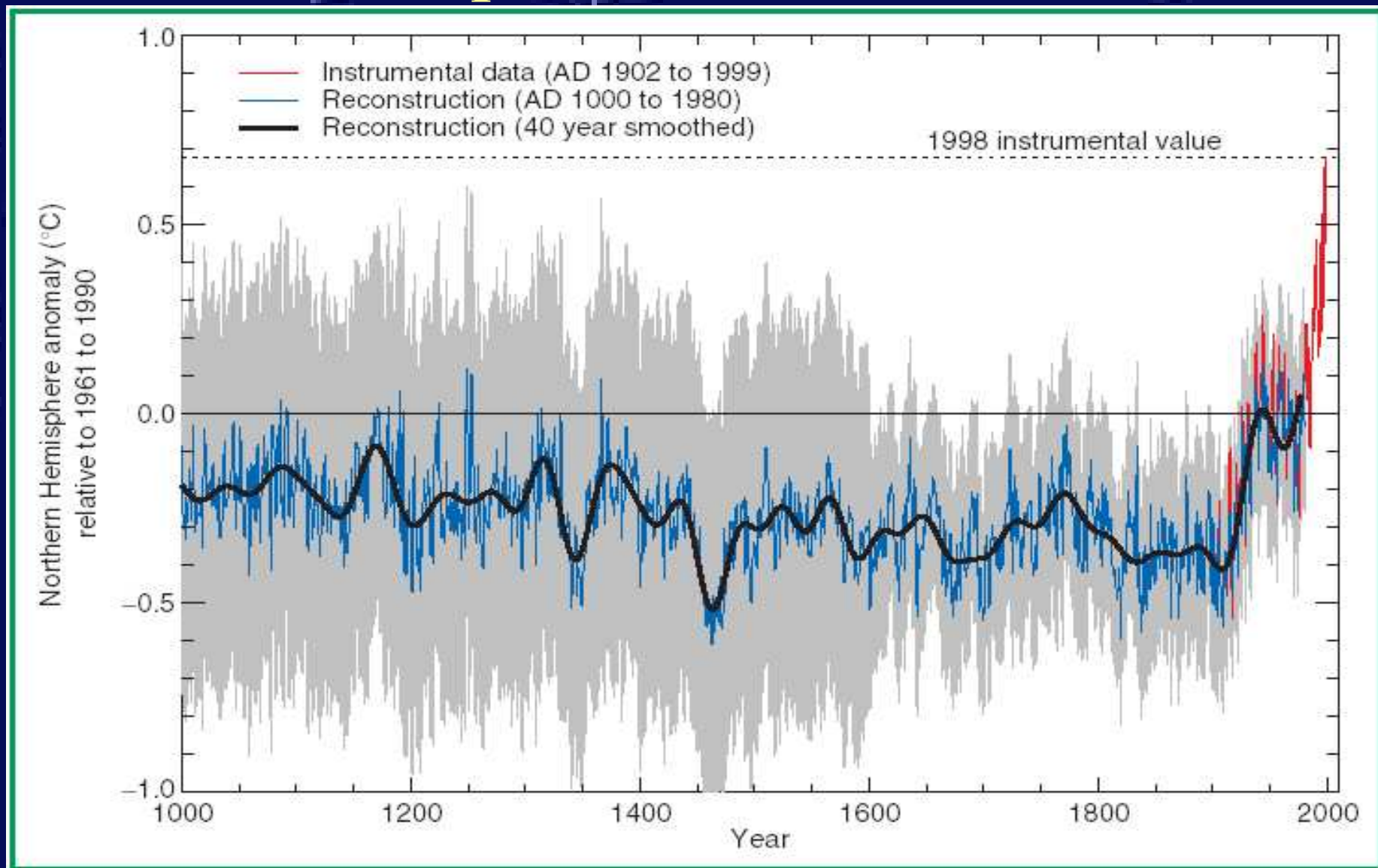


Figure 5: Millennial Northern Hemisphere (NH) temperature reconstruction (blue – tree rings, corals, ice cores, and historical records) and instrumental data (red) from AD 1000 to 1999. Smoother version of NH series (black), and two standard error limits (gray shaded) are shown. [Based on

From: Intergovernmental Panel on Climate Change (IPCC) - www.ipcc.ch

(FROM PREVIOUS LECTURES)

Light ?

..... Massless particles called **PHOTONS**

(Their speed is **$c=299\,792\,458$** m/s, in the vacuum)

They act as :

- **Particles** (interacting with matter)
- **Waves** (propagating)

Waves ?

(FROM PREVIOUS LECTURES)

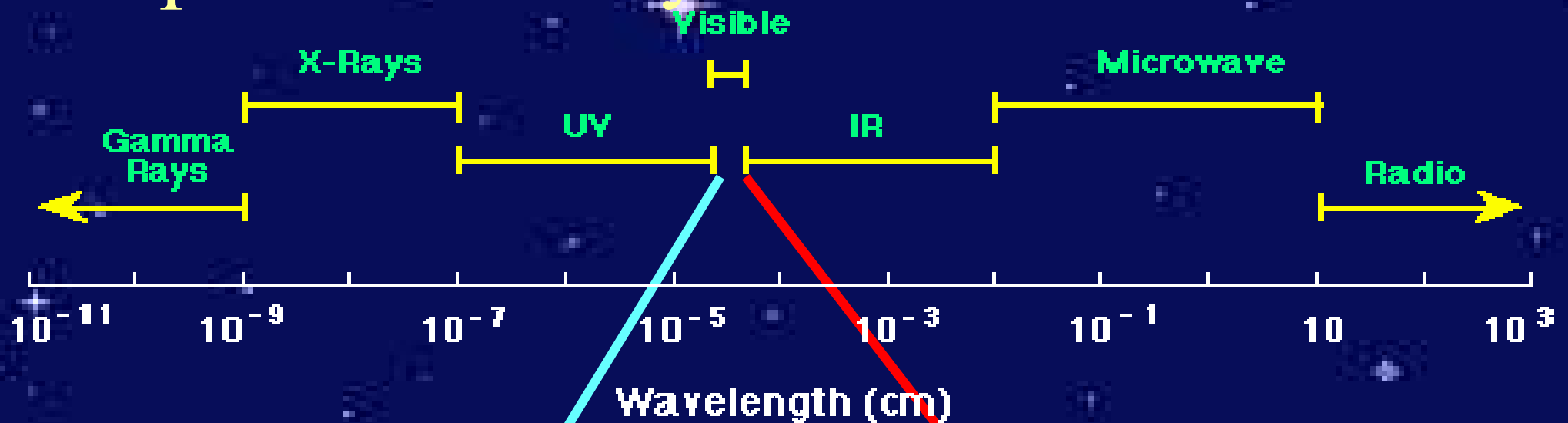
- Wavelength λ
- Frequency $\nu = c/\lambda$

Photon energy:

$$h\nu = hc/\lambda$$

(h = Planck's constant = 6.626×10^{-34} joule per sec)

The photons family: (FROM PREVIOUS LECTURES)



- Ultraviolet
- X Rays
- Gamma Rays

- Radio waves
- Microwave
- Infrared
- Visible

blue
400 nm
4000 Å

red
750 nm
7500 Å

Black Body light:

(FROM PREVIOUS LECTURES)

- Wavelength of the emission maximum

$$\lambda = \frac{2.8979 \times 10^{-3}}{T}$$

λ in meters

T in Kelvin

- overall emitted Flux

$$F = \sigma T^4$$

F in Watt and

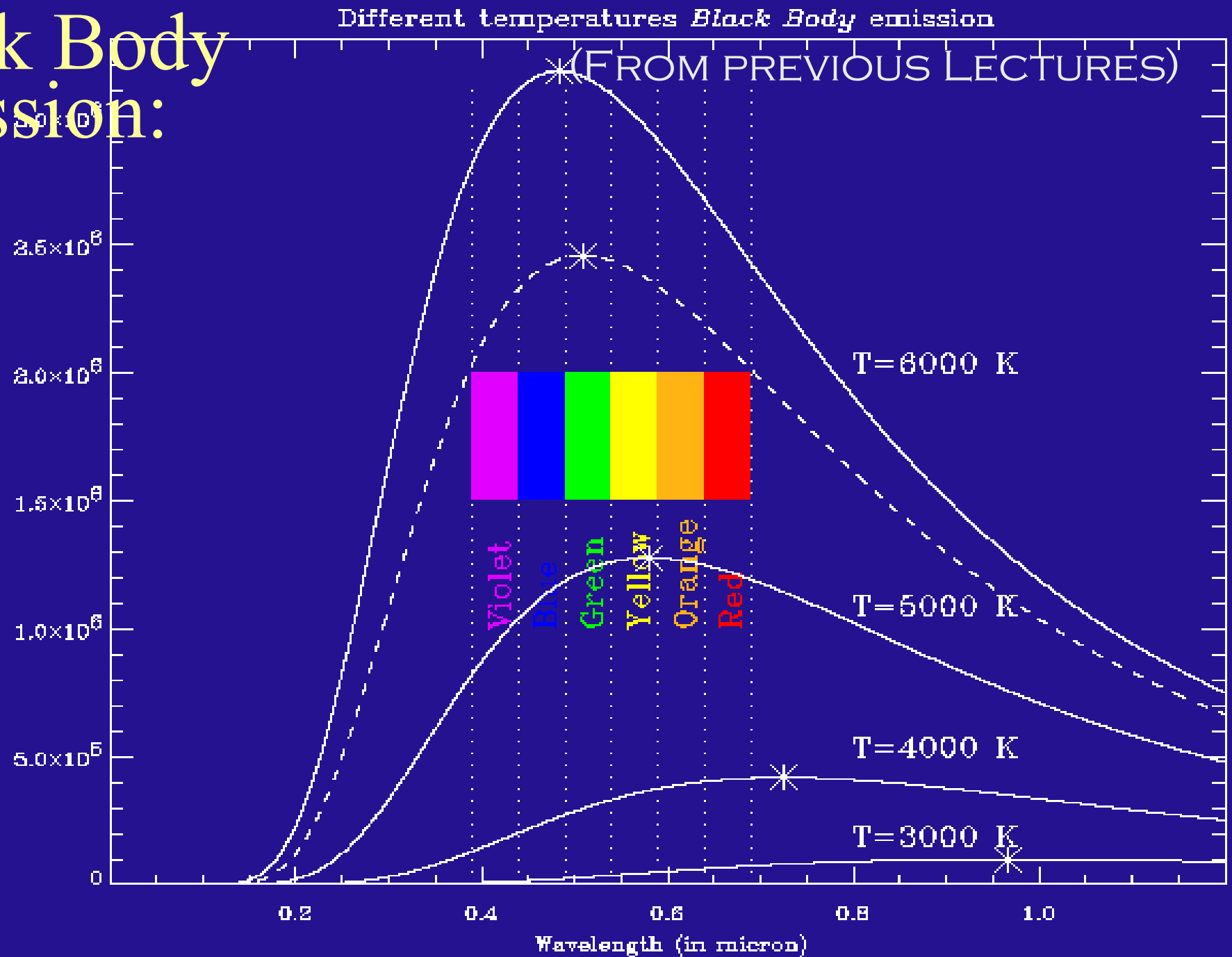
$$\sigma = 5.67 \times 10^{-8} \text{ W K}^{-4} \text{ m}^{-2}$$

- Flux at different λ (Planck's law)

$$F(\lambda, T) = \frac{2\pi hc^2}{\lambda^5} \frac{\Delta}{e^{\frac{hc}{\lambda kT}} - 1}$$

$$k = 1.3806 \times 10^{-23} \text{ j. per K}$$

Black Body Emission:



A human case:

(35 °C = 308.16 Kelvin)

(FROM PREVIOUS LECTURES)

$$\lambda_{\max} = 2.8979 \times 10^{-3} / T = 2.8979 \times 10^{-3} / 308.16 \approx 9.41 \times 10^{-6} \text{ m} = 9.41 \text{ } \mu\text{m}$$

$$F = \sigma T^4 = 5.67 \times 10^{-8} \times 308.16^4 \approx 511 \text{ W m}^{-2}$$

(cylinder, height of 1.75 *m*, diameter 0.45 *m*)

$$\begin{aligned} L &= F \times S = 511 \times 2.45 = 1252 \text{ W} = 0.3 \text{ Cal /sec} = 1080 \text{ Cal/hour} \\ &= 26000 \text{ Cal/day} \end{aligned}$$

**Don't fool yourself : this isn't the way to
lose weight !**

We are immersed in an environment at T_a

$$L_{\text{net}} = \sigma(T^4 - T_a^4) \times S = 216 \text{ W} = 4300 \text{ Cal/day}$$

(if we account for hairs and clothes, ≈ 2000)

The Stars: (T_{*} and R_{*} are surf. temperature and radius)

- Overall Flux at star surface (emitted power by 1 m² of star)

$$F_* = \sigma T_*^4$$

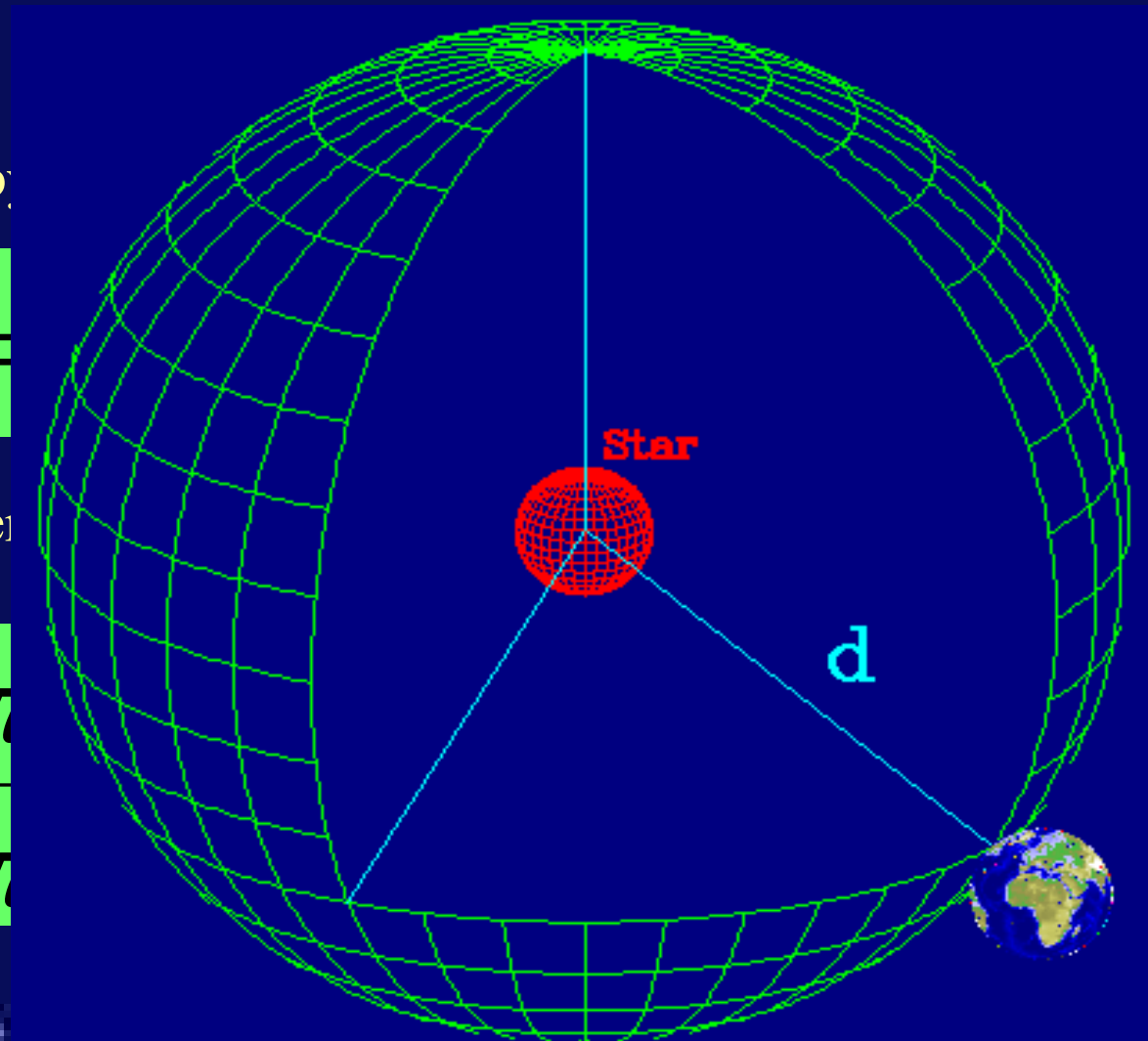
(FROM PREVIOUS LECTURES)

- Total Luminosity (emitted power by star)

$$L_* = 4\pi R_*^2 F_* =$$

- Total Flux at Earth (received power by Earth)

$$f = \frac{L_*}{4\pi d^2} = \frac{4\pi R_*^2 \sigma T_*^4}{4\pi d^2}$$



How can we get the stars temperature ?

(FROM PREVIOUS LECTURES)

For the SUN:

$$T_{\odot} = 5800 \text{ K}$$

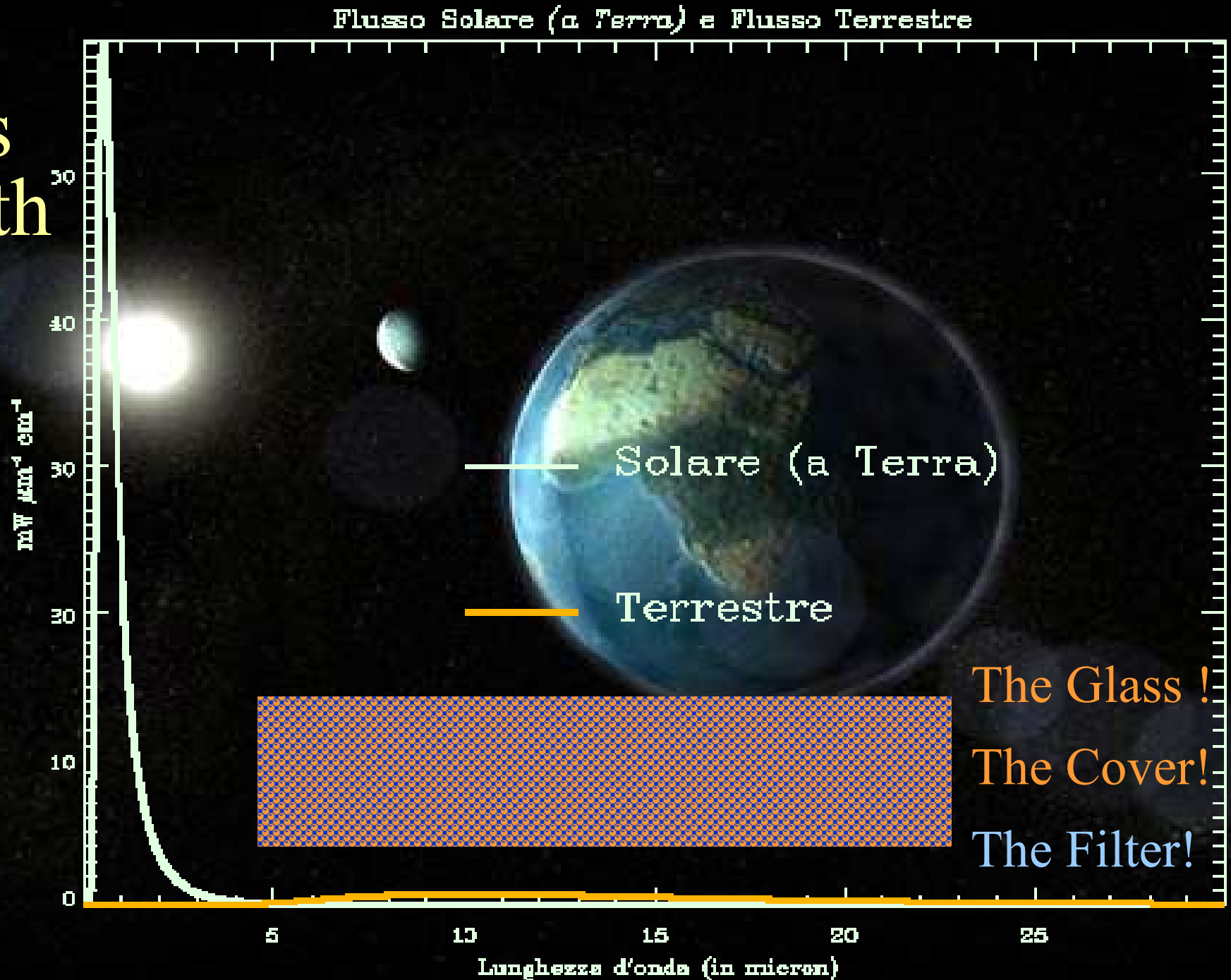
$$R_{\odot} = 6.96 \times 10^8 \text{ m}$$

$$L_{\odot} = 3.8 \times 10^{26} \text{ W}$$

$$d = 1.49 \times 10^{11} \text{ m}$$

$$f_{\odot} = 1.36 \text{ Kw}$$

The Fluxes at Earth !



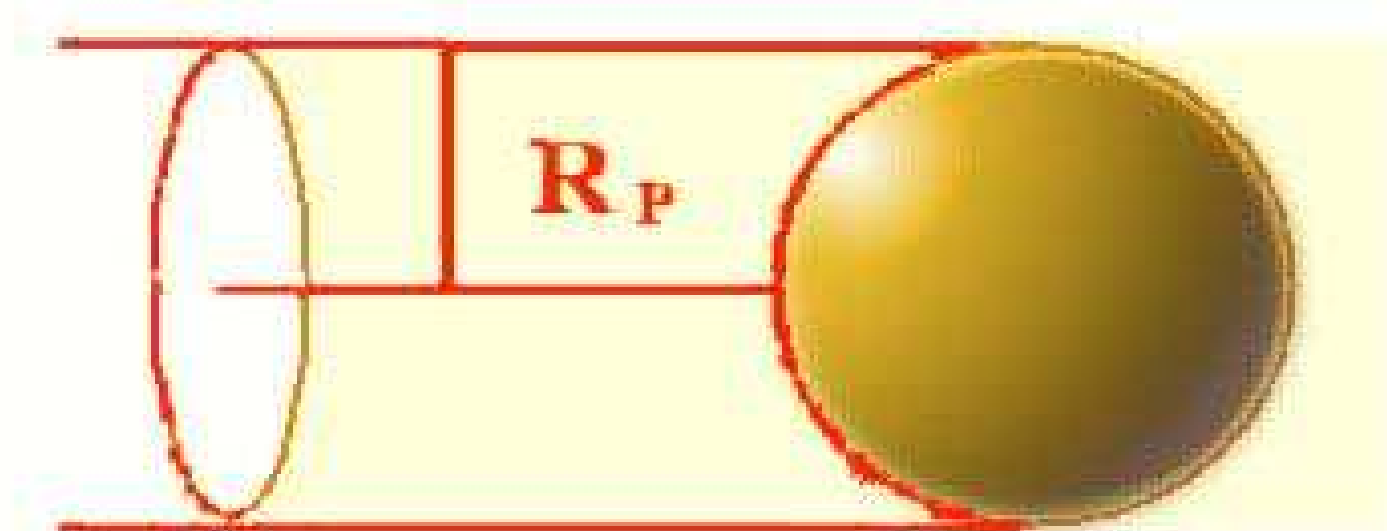
Quanta energia riceve un pianeta dal Sole?

$1 \text{ m}^2 \perp$ linea vista

$$\pi R_p^2 f$$

$$f = \frac{L_*}{4\pi d^2} = \frac{R_*^2}{d^2} \sigma T_*^4$$

S
O
L
E



non tutta la luce viene assorbita

Albedo ?

(.... i pianeti brillano di luce riflessa)



	Mercurio	Venere	Terra	Marte
Albedo	0,06	0,71	0,33	0,15
Distanza dal Sole (in M.Km)	57,9	108,2	149,6	227,9
Raggi (in Km)	2439	6052	6378	3397

Energia in ingresso (in un pianeta)

(principalmente nel visibile)

$$A_{ss} = \pi R_p^2 (1 - \alpha) f(T_*) = \pi R_p^2 (1 - \alpha) \frac{R_*^2}{d^2} \sigma T_*^4$$

Energia in uscita (da un pianeta)

(principalmente nell'infrarosso)

$$I_{rr} = S \varepsilon \sigma T_p^4$$

Temperatura di equilibrio di un pianeta

$$I_{rr} = A_{ss}$$

$$S \varepsilon \sigma T_P^4 = \pi R_P^2 (1 - \alpha) \frac{R_*^2}{d^2} \sigma T_*^4$$

• ε ???

• S (superficie che irradia) ??

$$T_P = T_* \sqrt[4]{\frac{\pi R_P^2 (1 - \alpha) R_*^2}{S \varepsilon d^2}}$$

Superficie che irradia: (1) ($\varepsilon = 1$, no Serra)

Ipotesi su pianeta:

- buon conduttore di calore,
- ruoti rapidamente,
- abbia una densa atmosfera
(irraggia da tutto il pianeta)

$$S = 4\pi R_P^2$$

$$T_P = T_* \sqrt[4]{\frac{(1 - \alpha) R_*^2}{4d^2}}$$

	Mercurio	Venere	Terra	Marte
T_P reale	623	753	287	250
T_P calcolato	441	241	252	217

Superficie che irradia: (2) ($\varepsilon = 1$, no Serra)

Ipotesi su pianeta:

- buon conduttore di calore,
- ruoti lentamente,
- non abbia densa atmosfera (irraggia dalla parte illuminata)

$$S = 2\pi R_p^2$$

$$T_p = T_* \sqrt[4]{\frac{(1 - \alpha) R_*^2}{2d^2}}$$

	Mercurio	Venere	Terra	Marte
T_p reale	623	753	287	250
T_p calcolato	525	286	300	258

Superficie che irradia: (3) ($\varepsilon = 1$, no Serra)

Ipotesi su pianeta:

- pessimo conduttore di calore,
- ruoti lentamente

(ogni area irraggia esclusivamente in proporzione all'energia assorbita)

$$S = \pi R_p^2$$

$$T_p = T_* \sqrt[4]{\frac{(1 - \alpha) R_*^2}{d^2}}$$

	Mercurio	Venere	Terra	Marte
T_p reale	623	753	287	250
T_p calcolato	624	340	357	307

Continua ...

la TERRA:

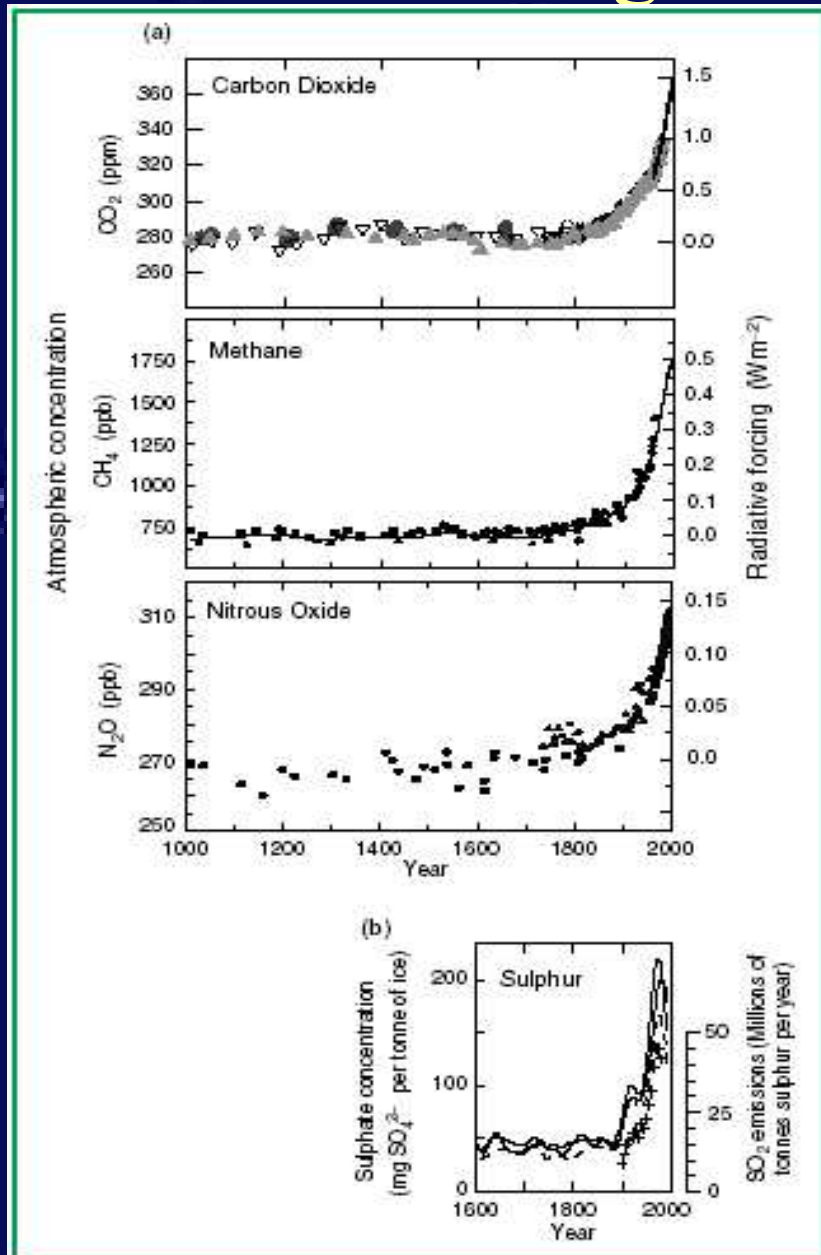
- buon conduttore di calore,
- ruota rapidamente,
- ha una densa atmosfera

($\varepsilon=1$) T_p reale = 287 - T_p calcolato = 252

- Quanto vale ε ?
- Qual è la T se ε diminuisce del 10% ?

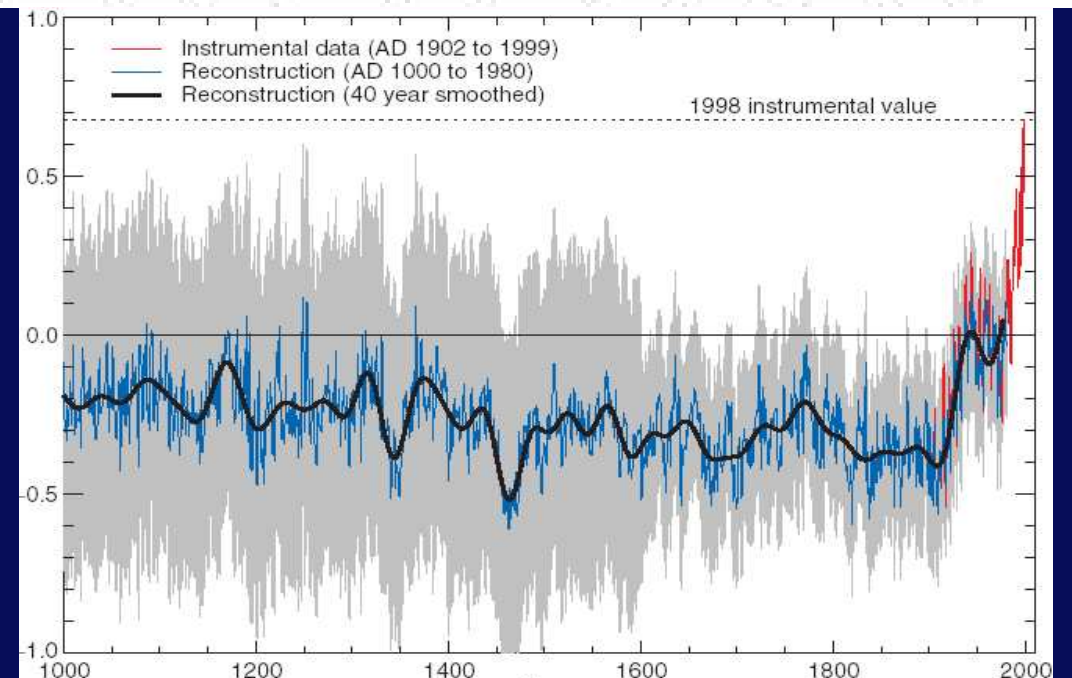
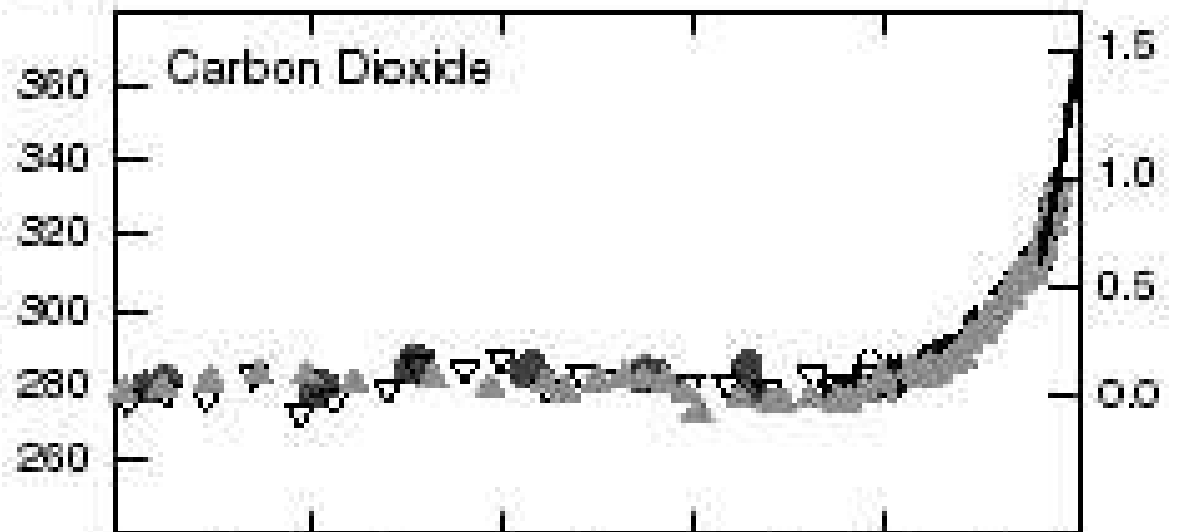
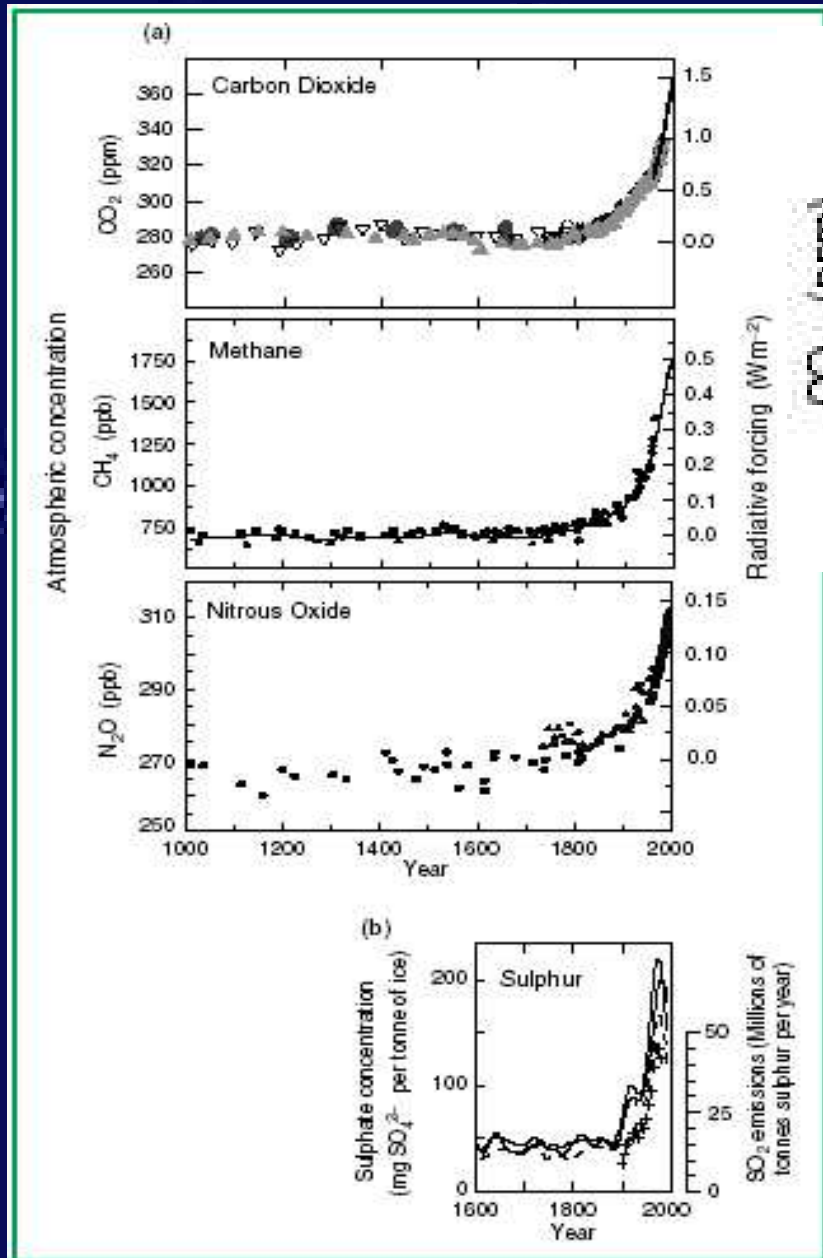
$\varepsilon = 59\%$ ---- $T = 294 \text{ K}$

Concentrazioni gas *serra* 1000-2000:



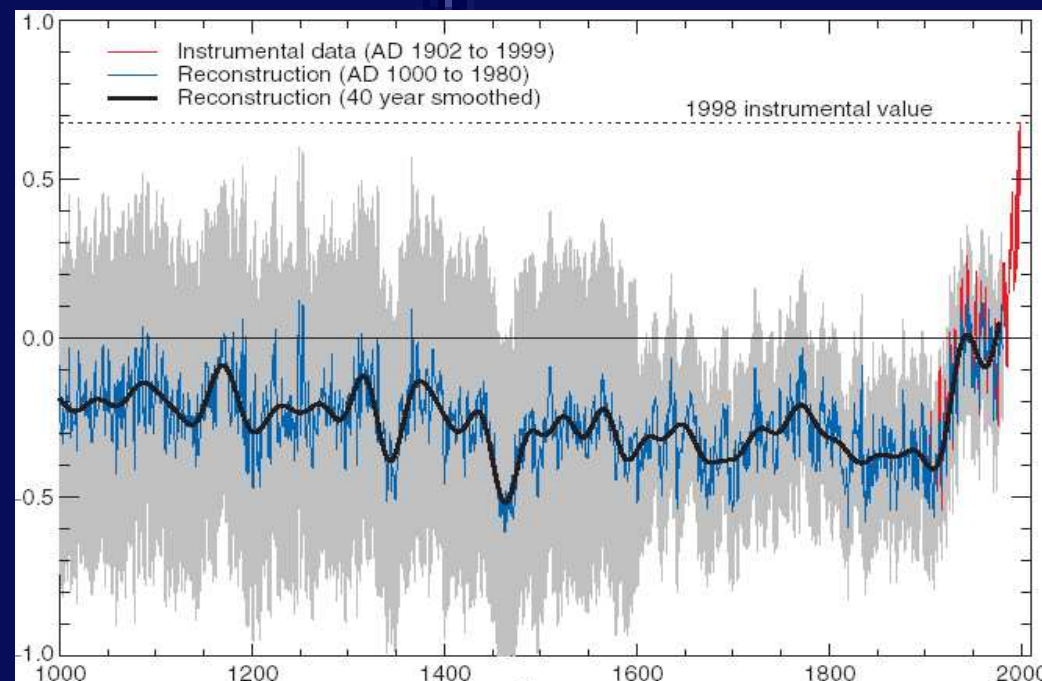
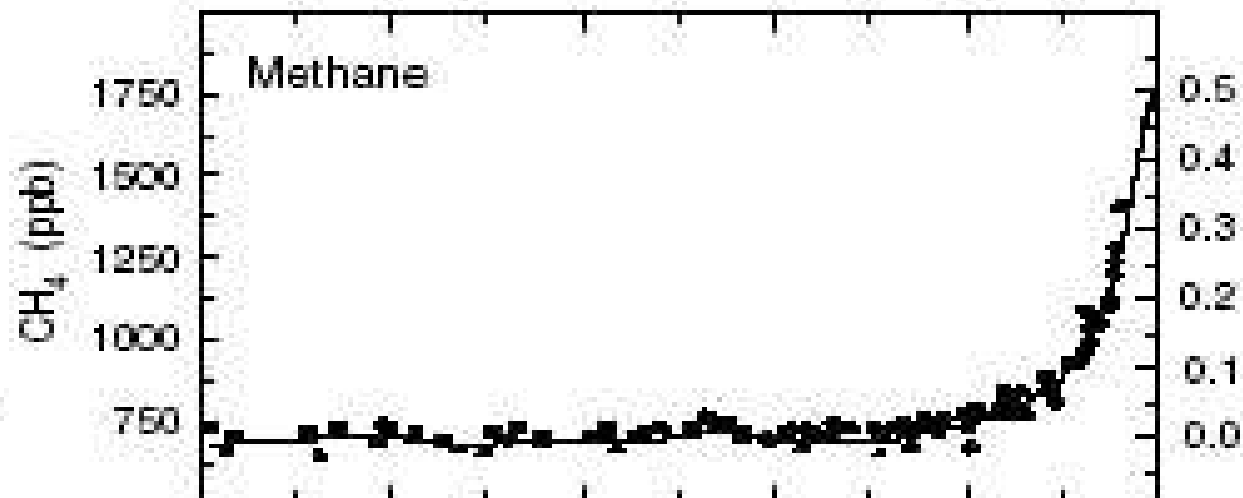
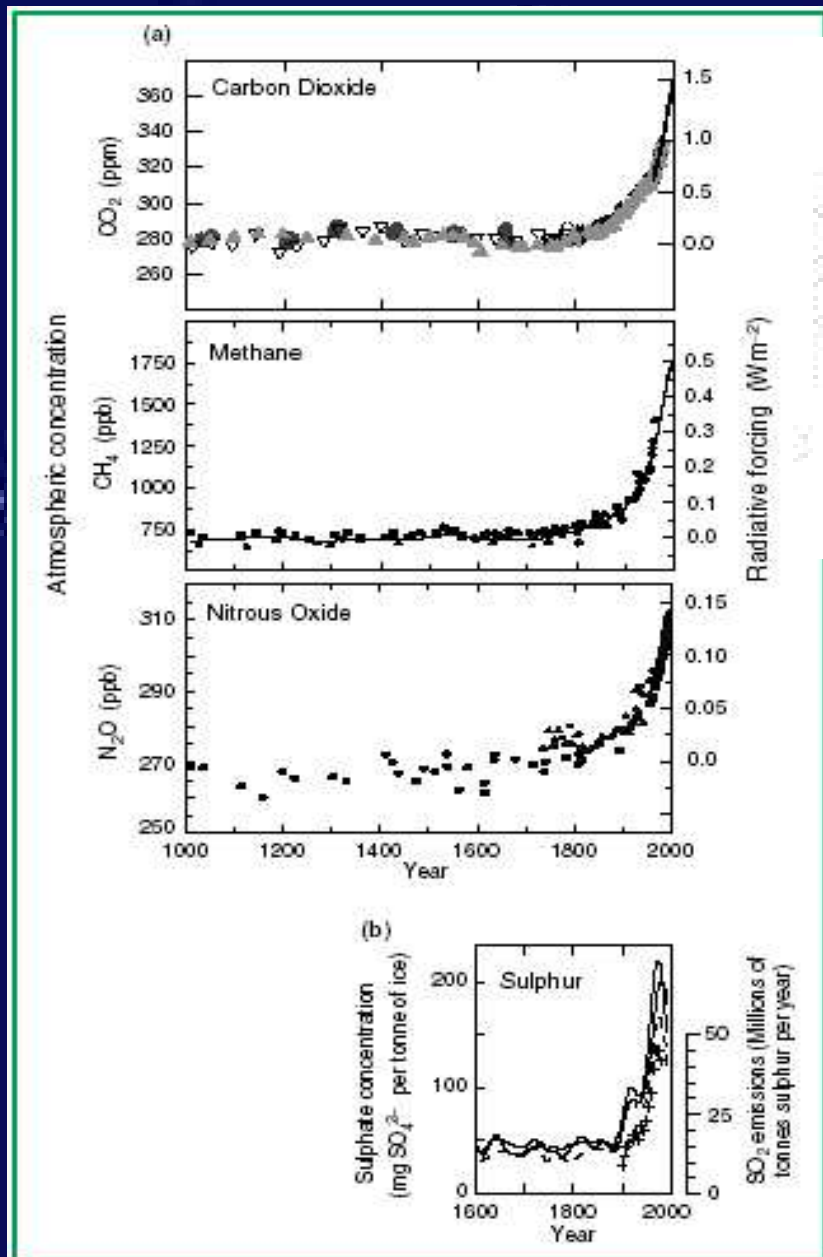
From: Intergovernmental Panel on Climate Change (IPCC) - www.ipcc.ch

Concentrazione CO₂ 1000-2000:



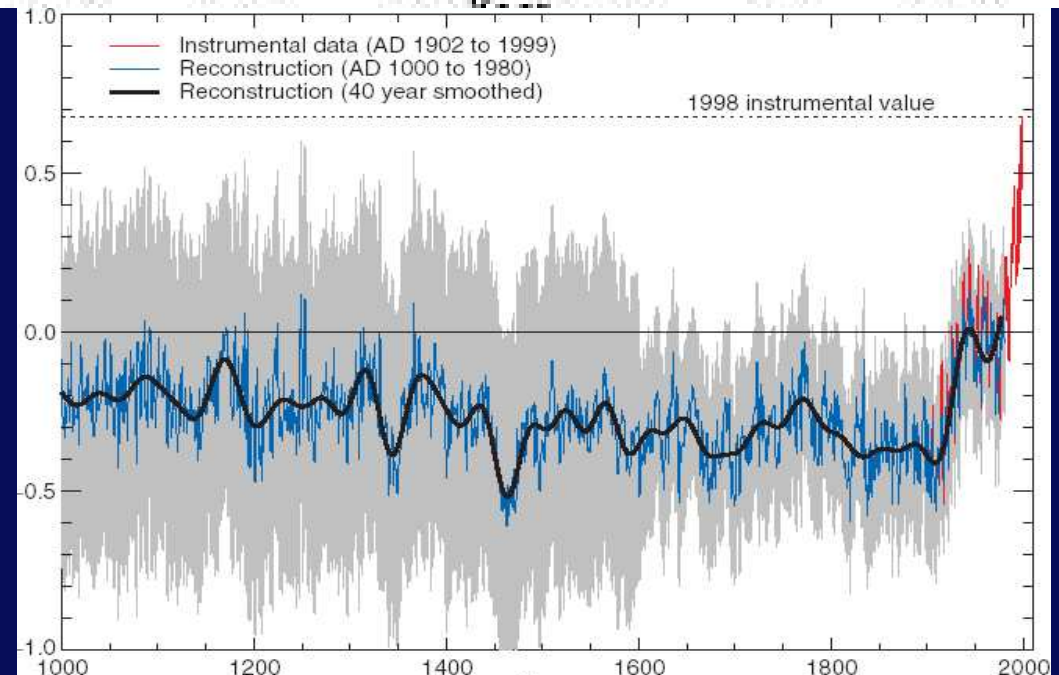
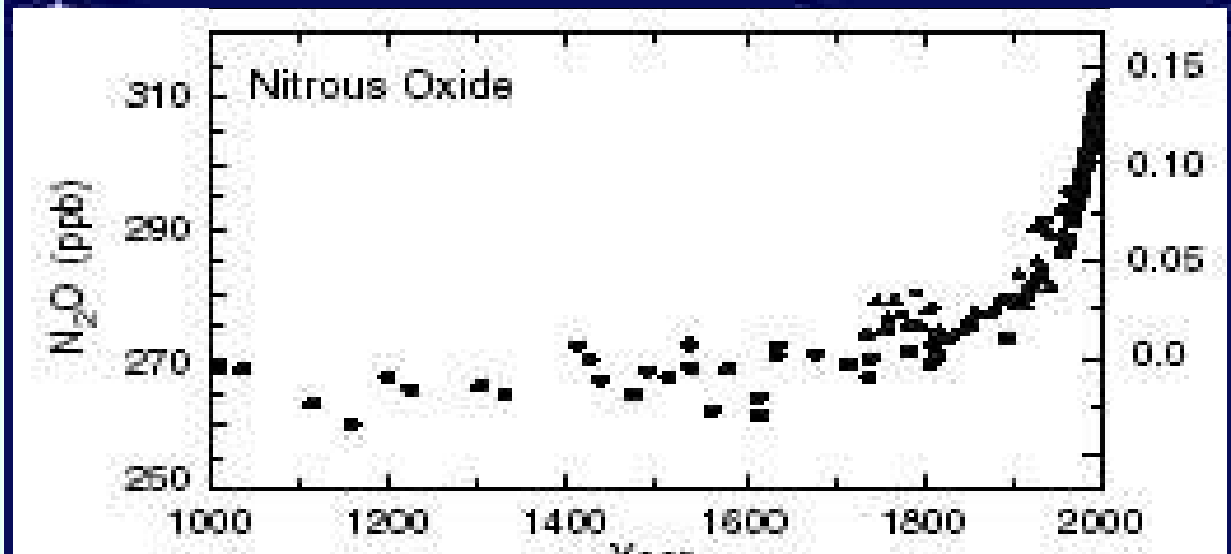
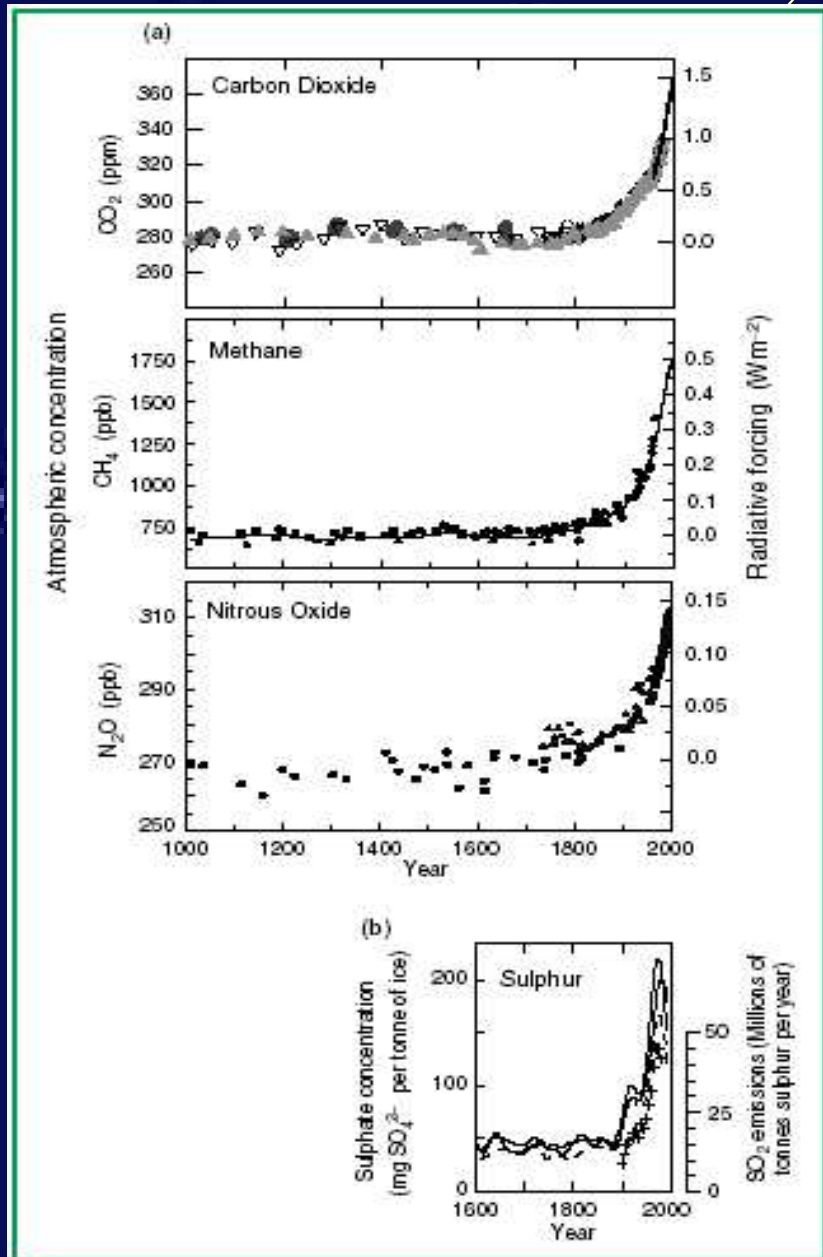
From: Intergovernmental Panel on Climate Change (IPCC) - www.ipcc.ch

Concentrazione CH₄ 1000-2000:



From: Intergovernmental Panel on Climate Change (IPCC) - www.ipcc.ch

Concentrazione N₂O 1000-2000:



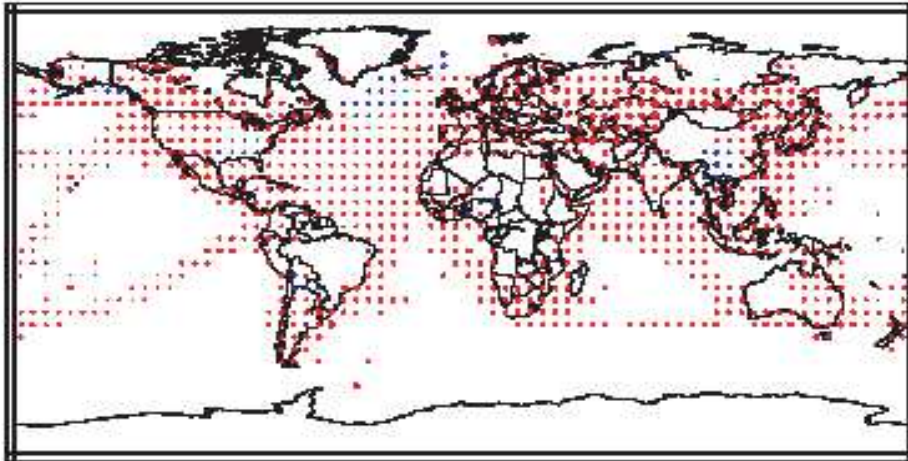
From: Intergovernmental Panel on Climate Change (IPCC) - www.ipcc.ch

Contributi dei gas serra alla Temperatura :

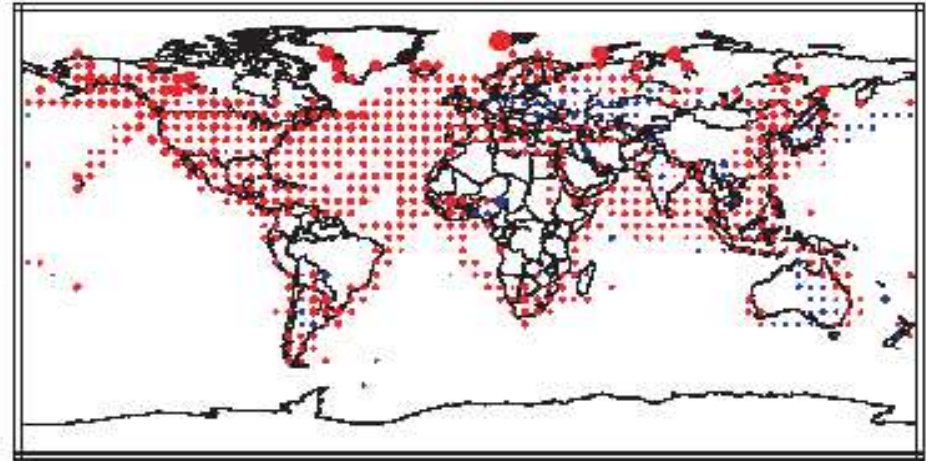
Gas Serra	Forzatura Emissione (W/m ²)	ΔT	ΔT Era Ind.
H ₂ O	144	32,5	-
CO ₂	7,8	1,8	0,4
CH ₄	0,88	0,2	0,1
N ₂ O	1,2	0,3	0,04
Altri	1,2	0,3	0,1

Andamenti locali temperatura 1900-2000:

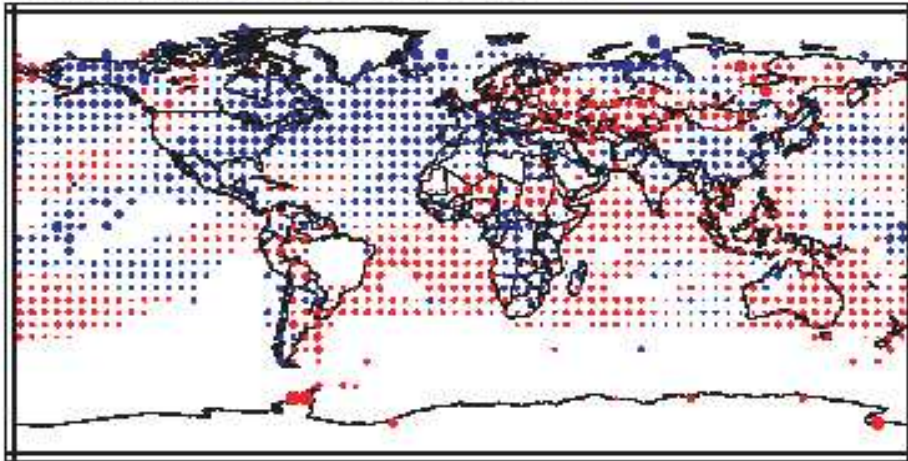
(a) Annual temperature trends, 1901 to 2000



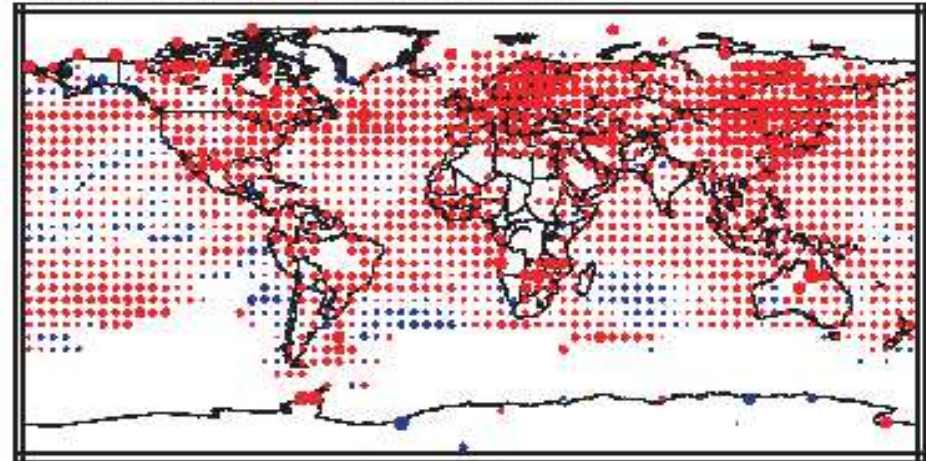
(b) Annual temperature trends, 1910 to 1945



(c) Annual temperature trends, 1946 to 1975

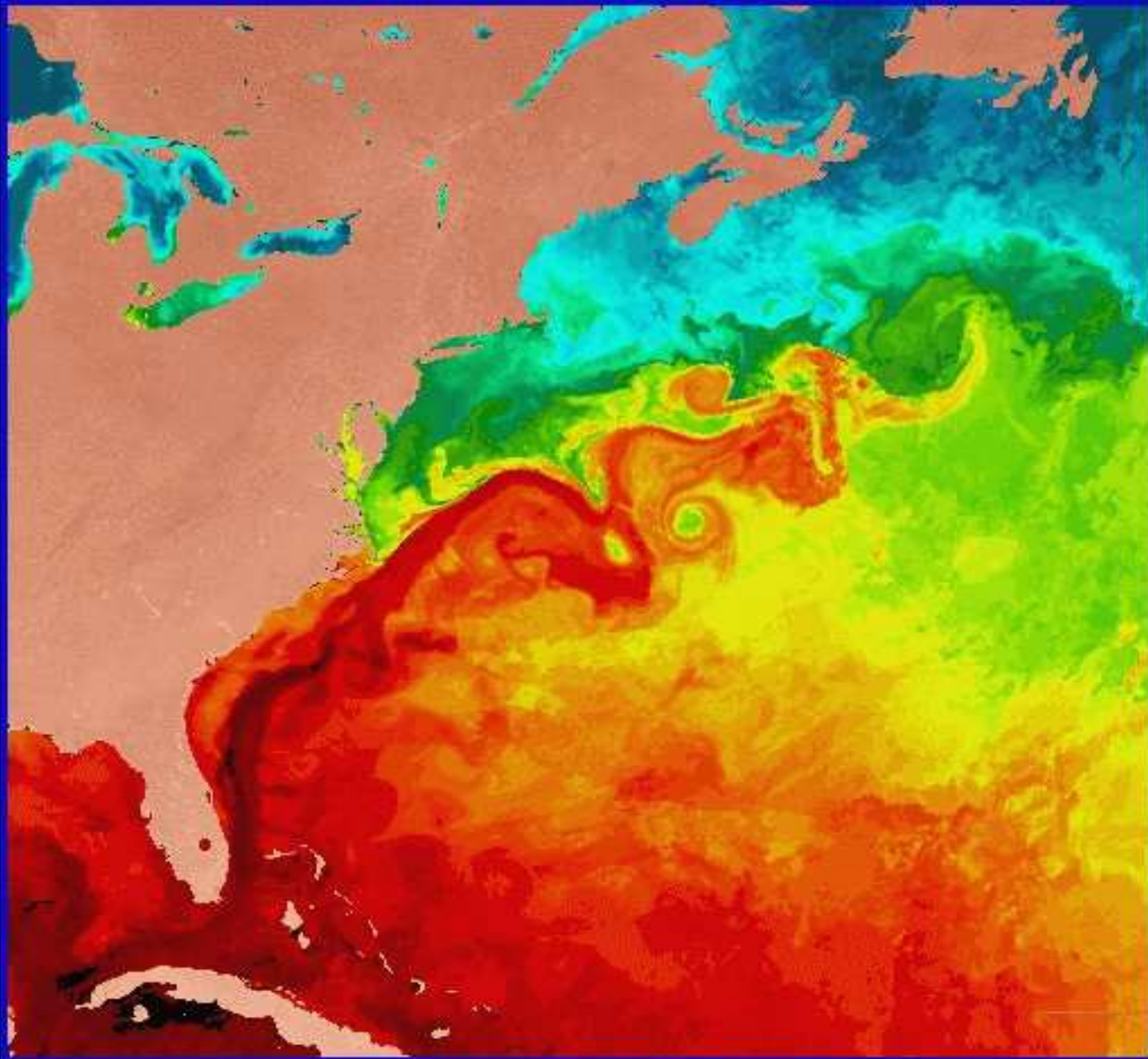


(d) Annual temperature trends, 1976 to 2000

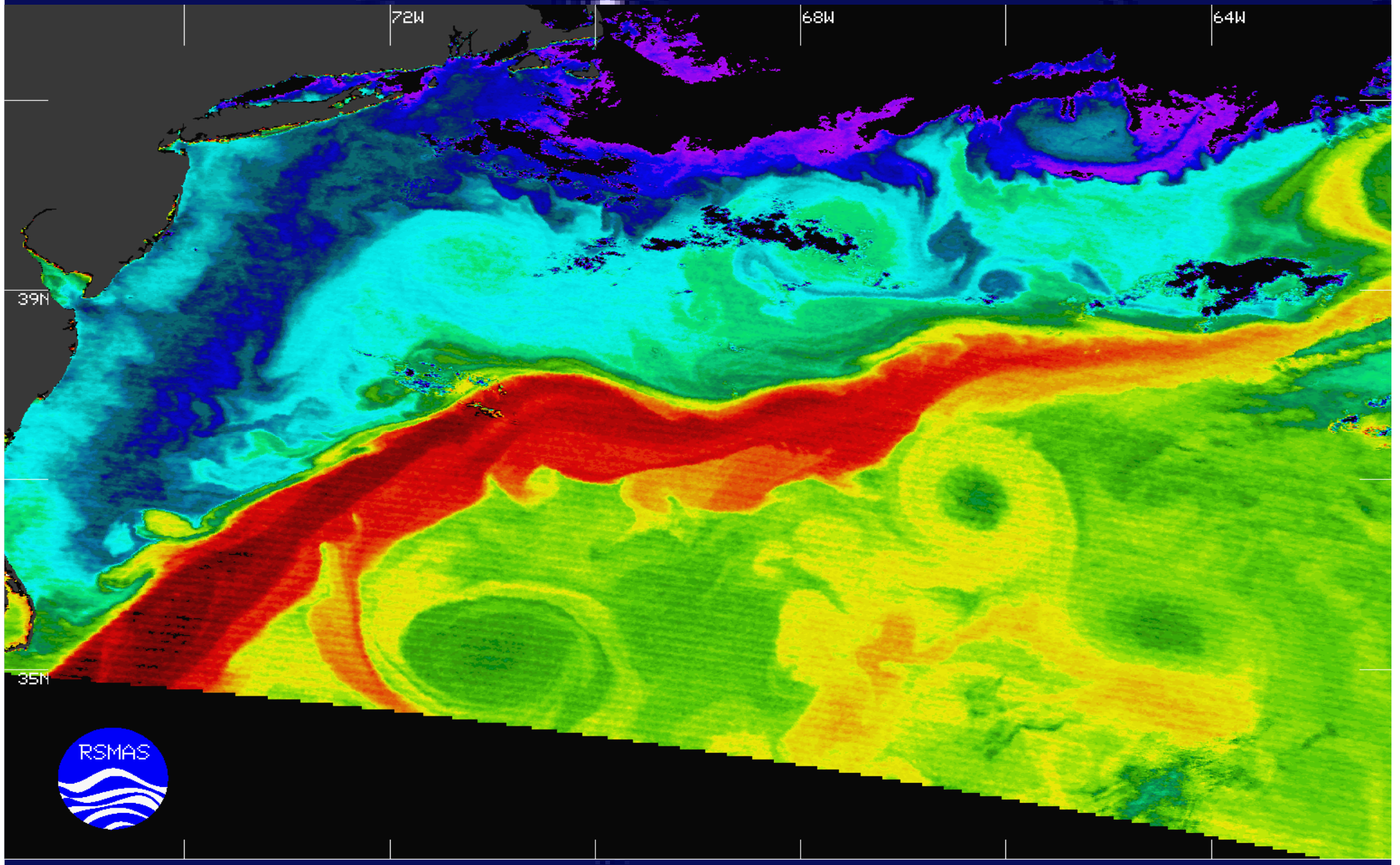


-1 -0.8 -0.6 -0.4 -0.2 0 0.2 0.4 0.6 0.8 1
Trend ($^{\circ}\text{C}/\text{decade}$)

La Complessità del Clima



La Complessità del Clima



La Complessità del Clima



Il Tamigi gelato
(*Hendrick Avercamp, 1585-1663*)