

# Course of General Astronomy



Gulu University

Naples FEDERICO II University



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## Mass of Andromeda Galaxy

## Radial Velocity (along L. of S.) at various distances from the center of Andromeda Galaxy

Dist. '	V Km/s	Dist. '	V Km/s	Dist. '	V Km/s	Dist. '	V Km/s
-120	-460	-15	-340	+2	-250	+28	-120
-100	-500	-13	-340	+6	-220	+29	-120
-96	-530	-10	-310	+5	-210	+46	0
-80	-600	-8	-350	+4	-205	+66	+70
-65	-580	-7	-330	+10	-260	+70	+60
-70	-570	-6	-370	+12	-250	+80	+100
-50	-530	-3	-360	+12	-210	+96	+80
-29	-480	-3	-340	+14	-180	+100	+30
-30	-440	-2	-305	+15	-180	+107	-50
-25	-415	+8	-290	+16	-170	+120	-50
-20	-390	+5	-280	+22	-125		
-16	-360	+2	-250	+21	-100		

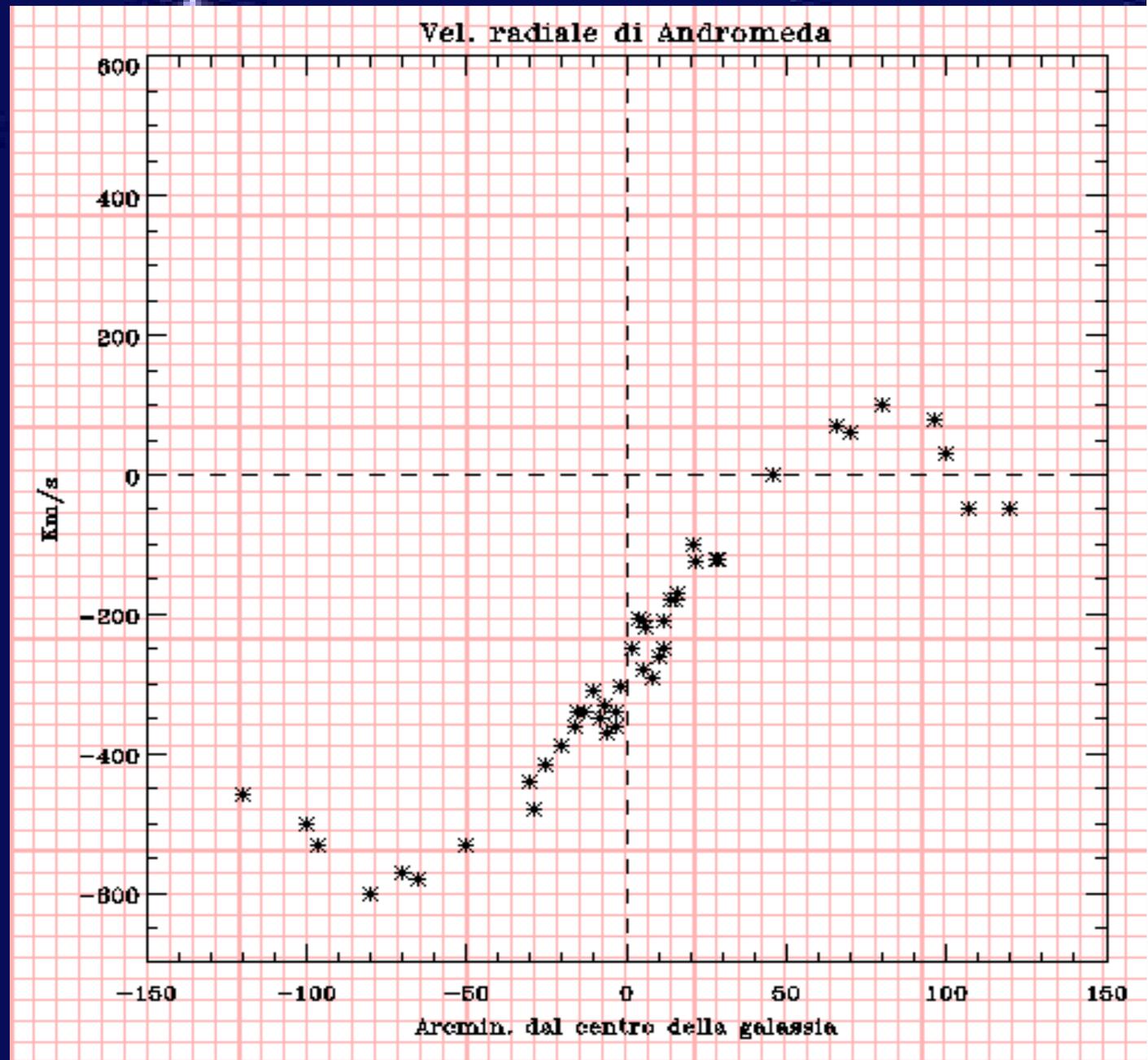
Can you see some strange behaviour??

# Plot of experimental data

Excess of  
approaching  
velocities

Why ??

Center of Mass  
motion (relative  
velocity Sun -  
galaxy)



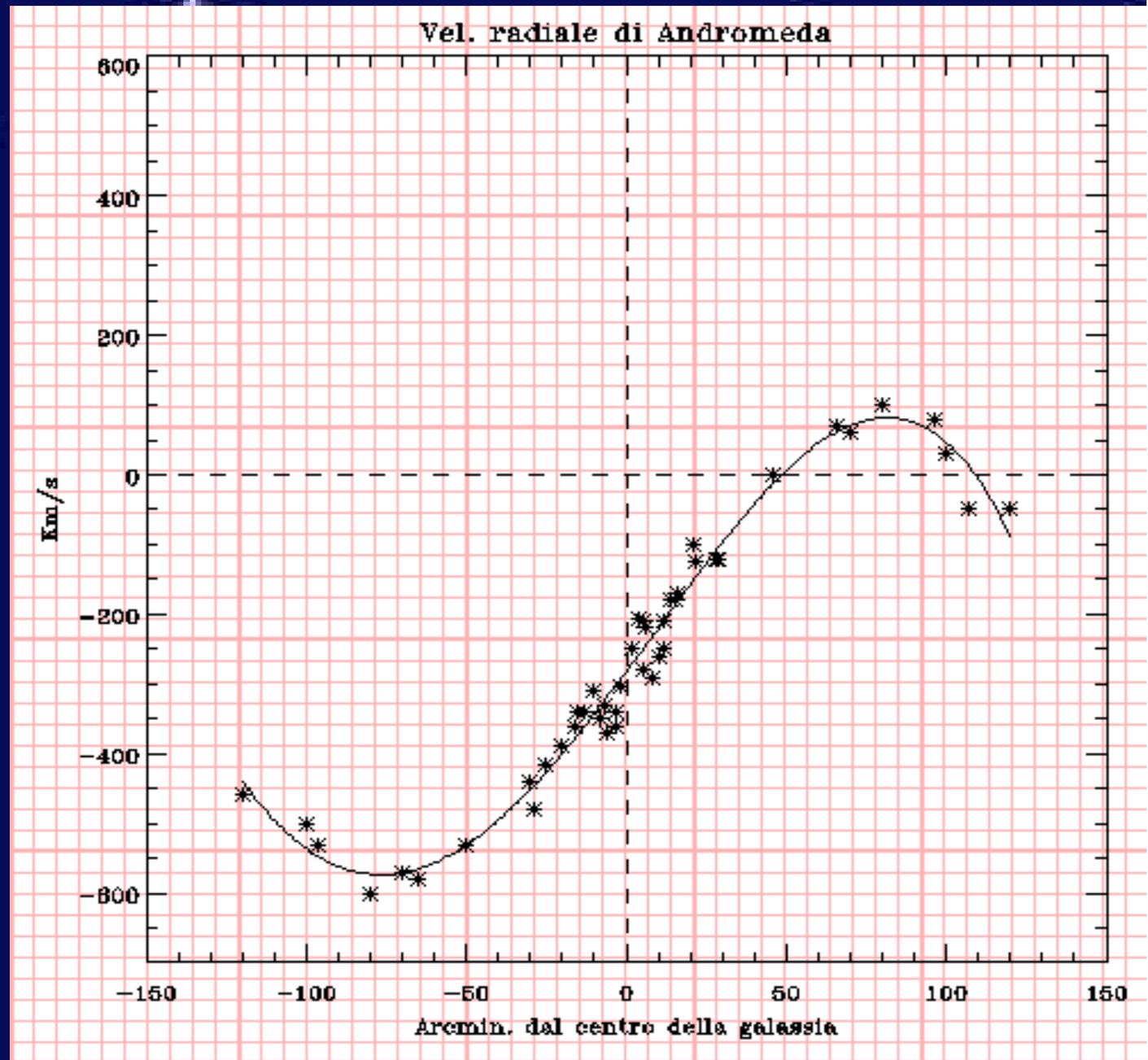
# Plot of experimental data

Excess of  
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Center of Mass  
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Pay attention to  
the mean value  
!



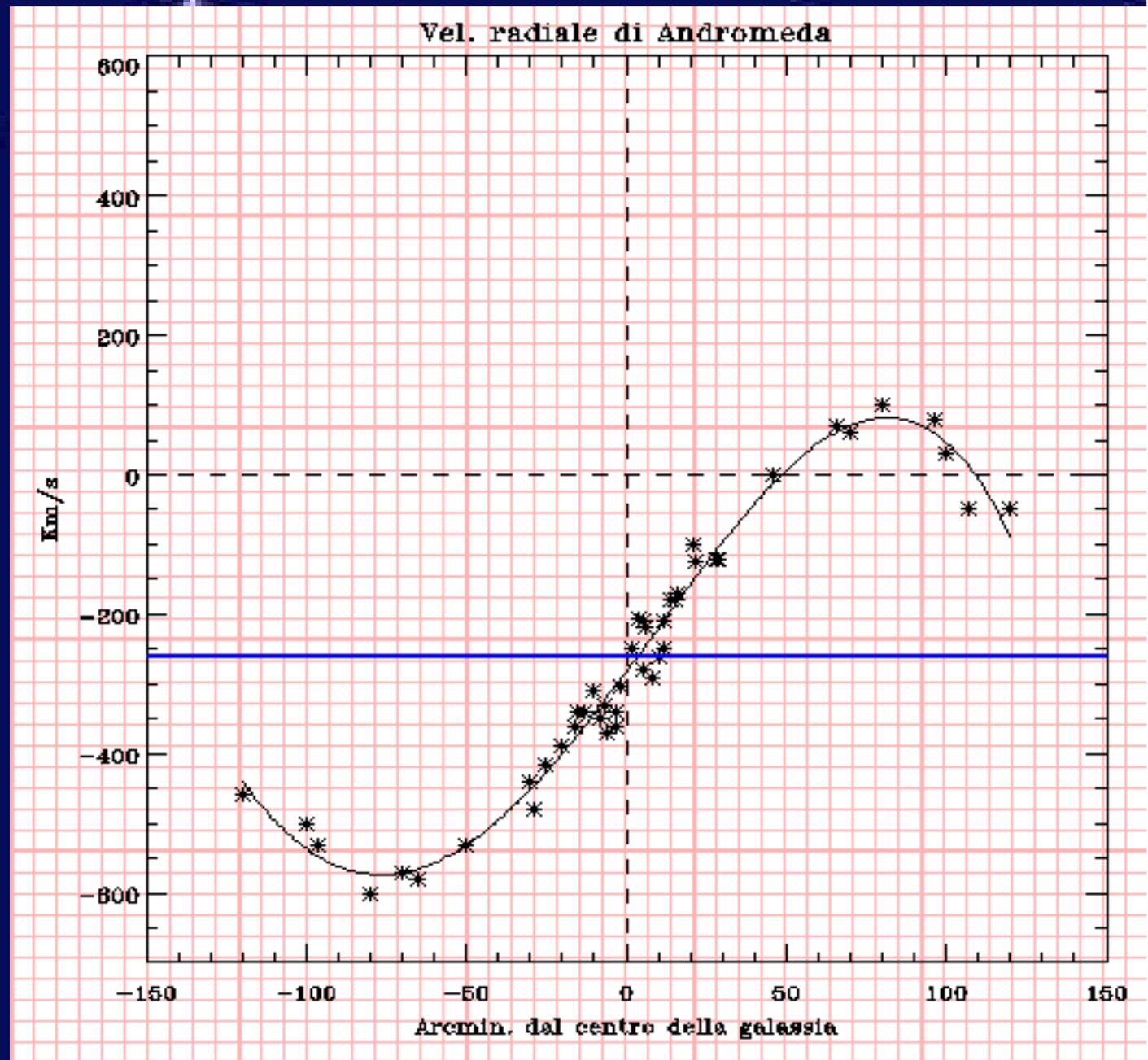
# Plot of experimental data

Excess of  
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Why ??

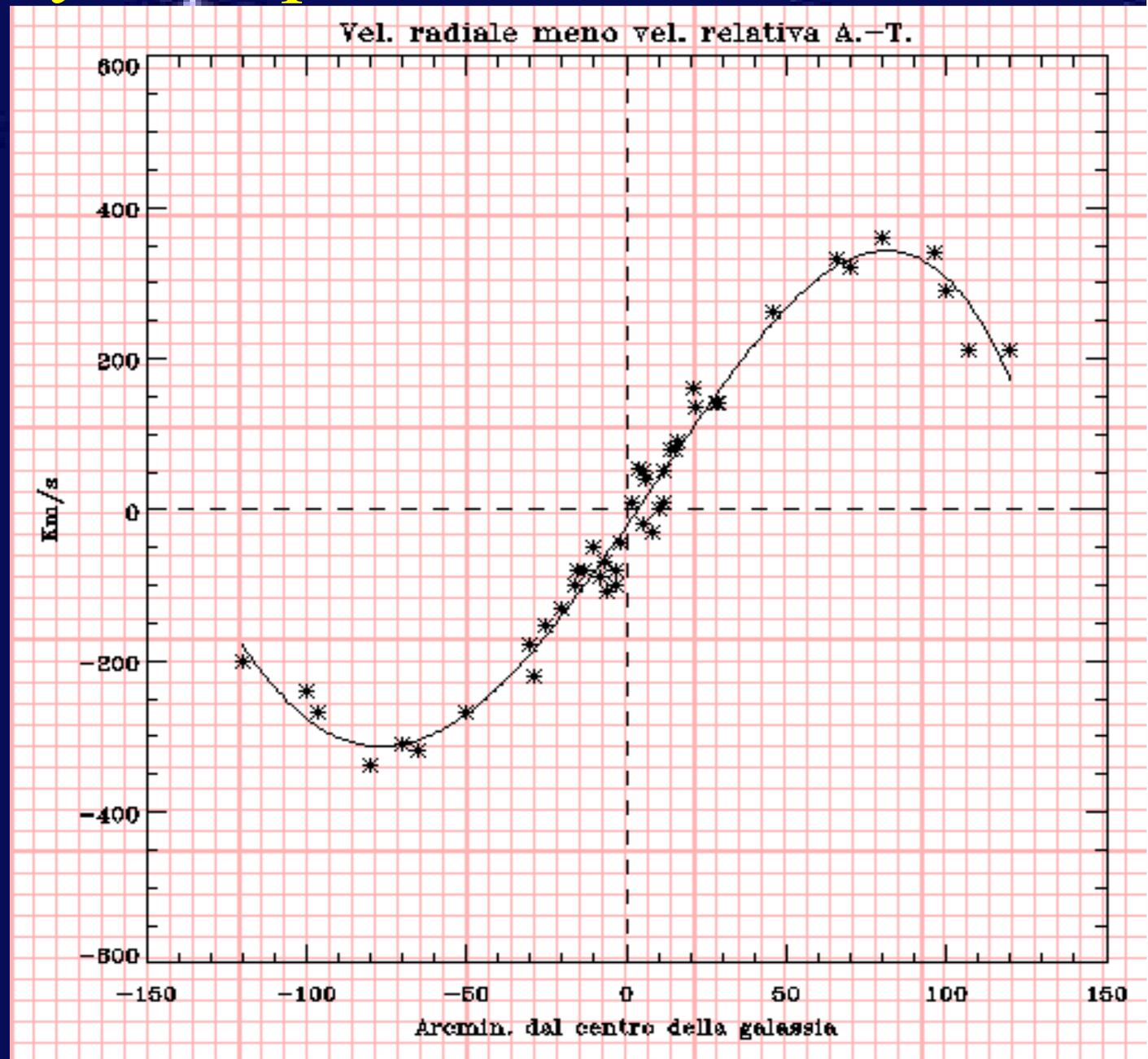
Center of Mass  
motion (relative  
velocity Sun -  
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Pay attention to  
the mean value  
!



# Rotation Velocity Component

Why this  
strange  
behaviour ?



## Involved Concepts Nodes:

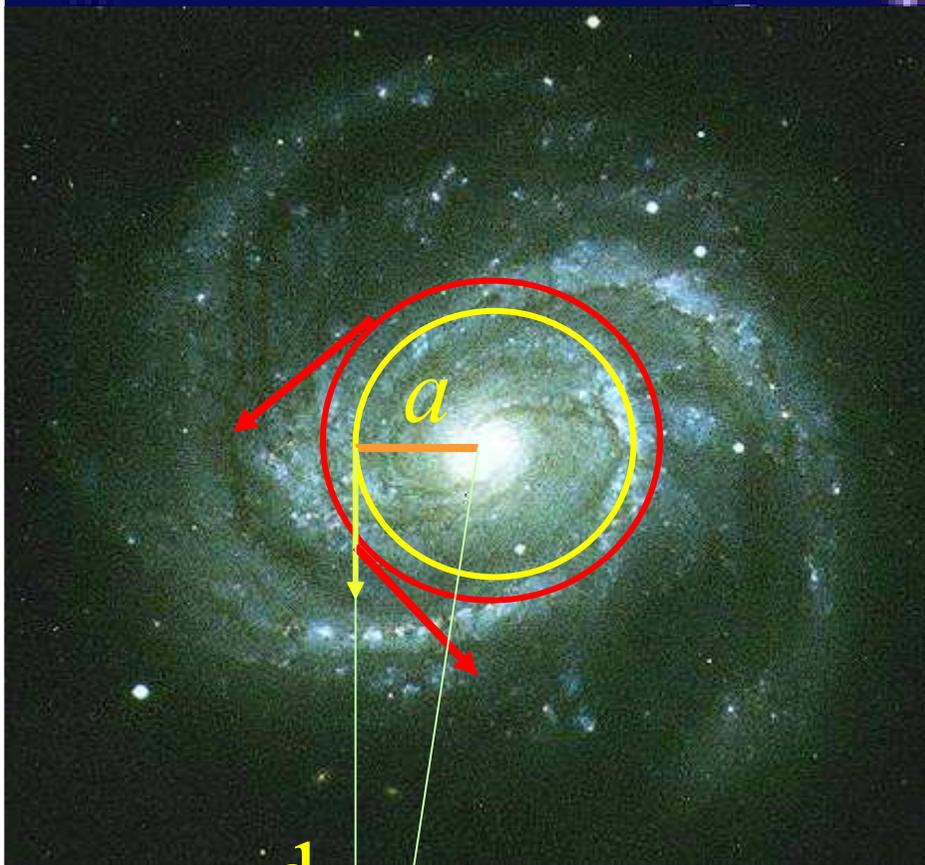
1) velocity along the Line of Sight (radial)

2) angular distance

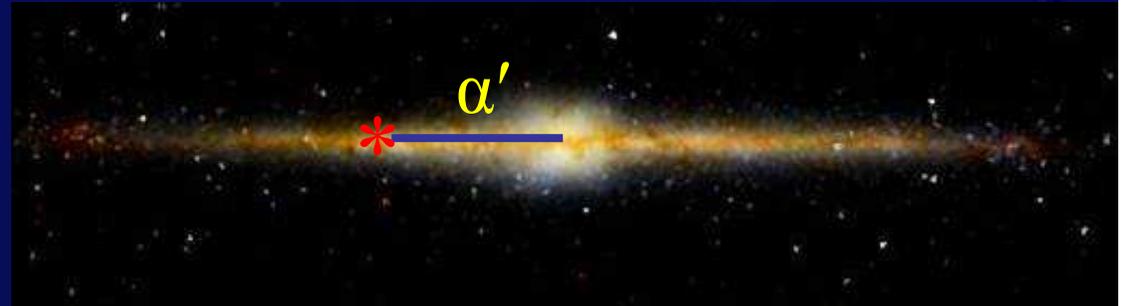
3) rotation model

.... (Keplerian motion)

# Radial Velocity



$$a = d\alpha'/3437.7$$



## III Kepler's Law

$$T^2 = (2\pi)^2 a^3 / GM_a$$

$$V_a = 2\pi a / T = 2\pi a / 2\pi a \sqrt{a / GM_a} = \sqrt{GM_a / a}$$

# The strange behaviour:

constant density (*model*)

$$M_a = (4/3)\pi\rho a^3 \Rightarrow V_a = \sqrt{\frac{4}{3}\pi a^3 \rho G / a} = a \sqrt{\frac{4}{3}\pi\rho G}$$

when the galaxy is ended  $M_a = M_{\text{Andr}}$

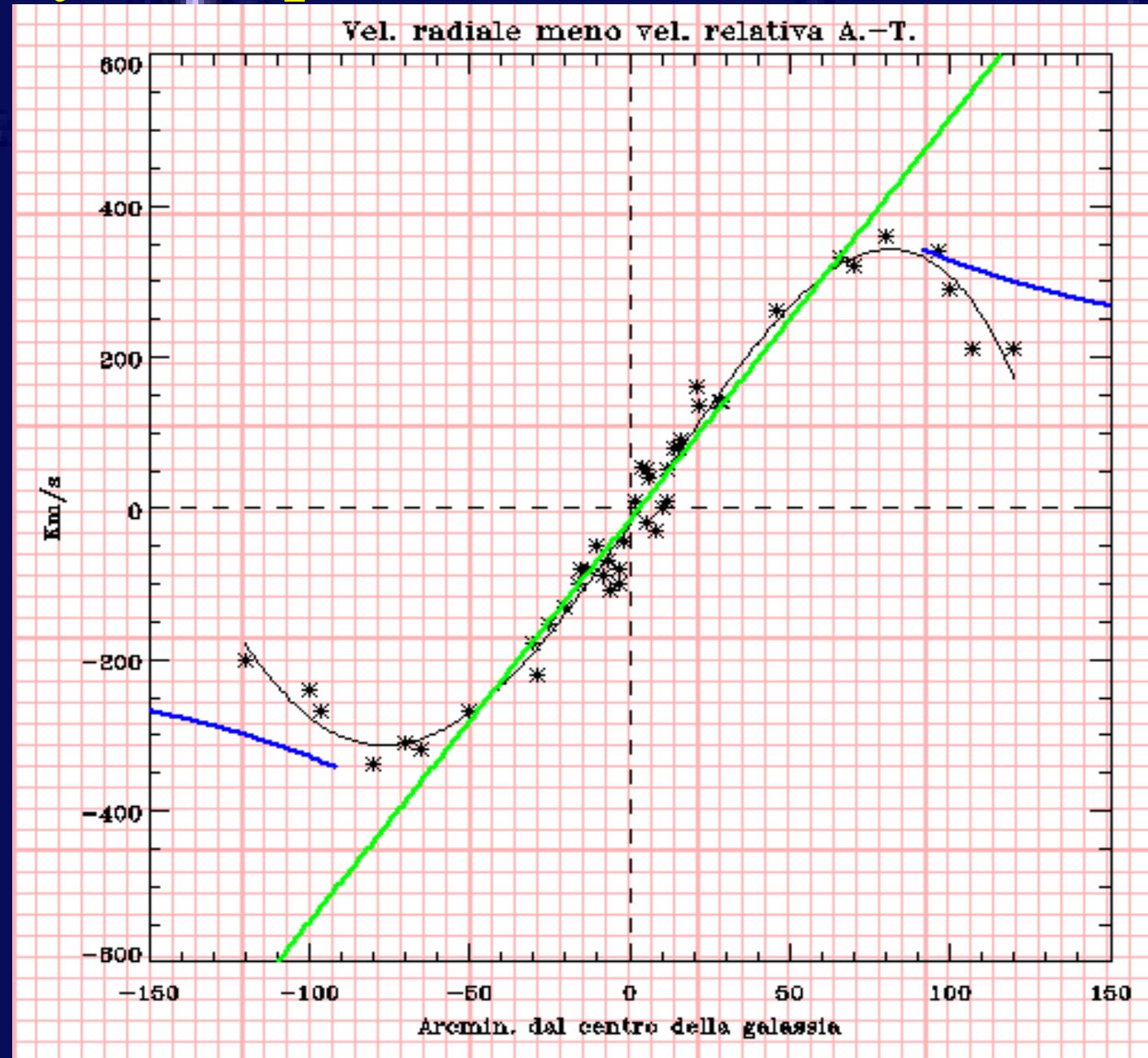
$$\Rightarrow V_a = \sqrt{GM_{\text{Andr}} / a} = \sqrt{GM_{\text{Andr}}} \sqrt{\frac{1}{a}}$$

# Rotation Velocity Component

The reason for strange behaviour :

Green: linear dependence from distance (densità cost.)

Blue: region inverse square of distance (galaxy ended)

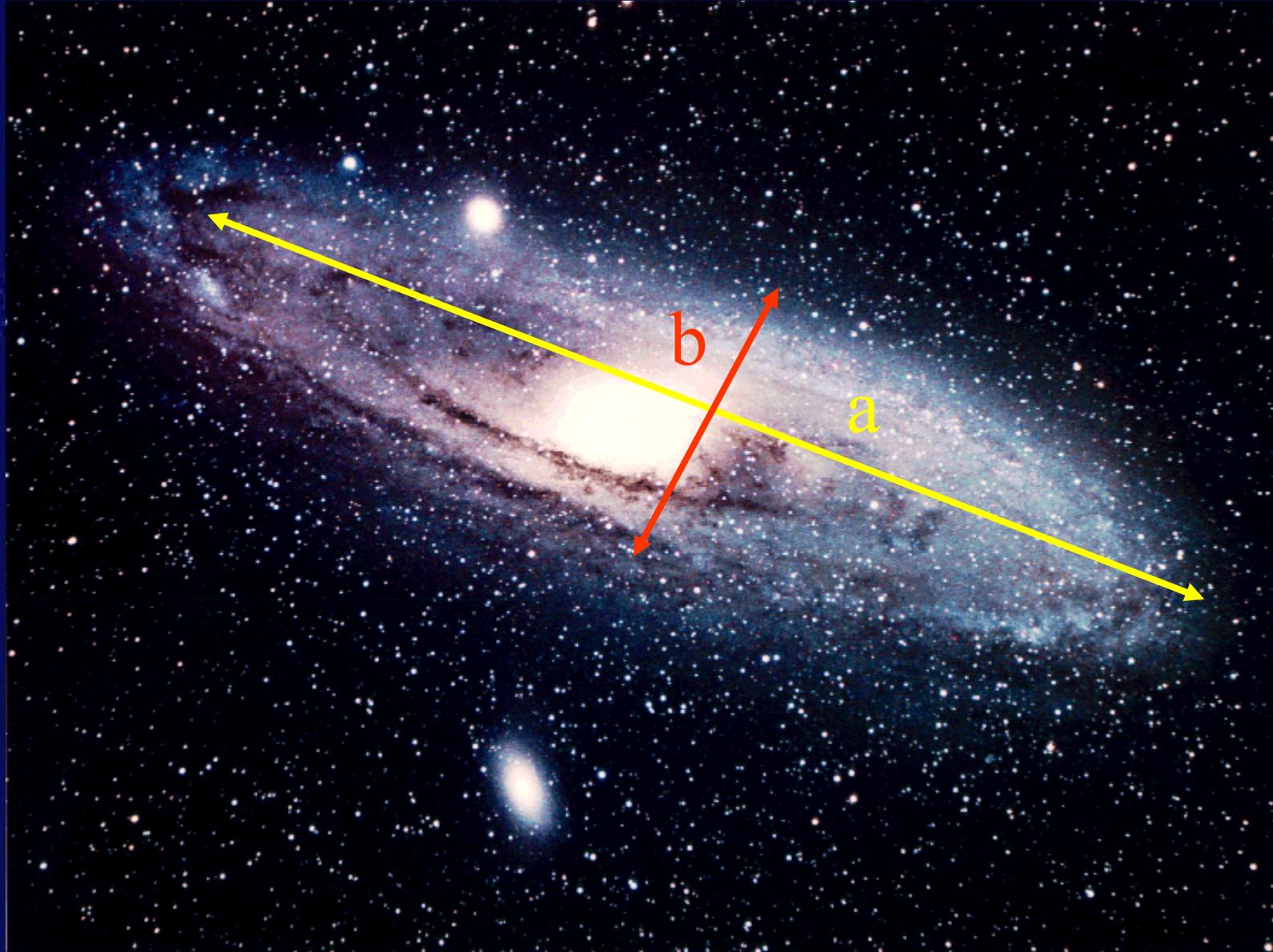


You have to select region having  $M_a \approx M_{\text{Andr}}$

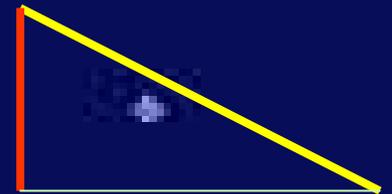
$M_{\text{Andr}}$ : excess o defect determination ?

Did you see an Andromeda galaxy imagine ?

There is :



*model:*  
*circular*  
*disk*  
*galaxy*



$V_{\text{obs}}$



$V_{\text{real}}$

# Steps

1. Data plot
2. Linear fitting of central part: CM vel.
3. Selection of appropriate regime for  $M_a$
4. Use of galaxy both side (mean value)
5. Mass estimation
6. Excess or defect determination ?
7. Explain (*shortly*) the used methods