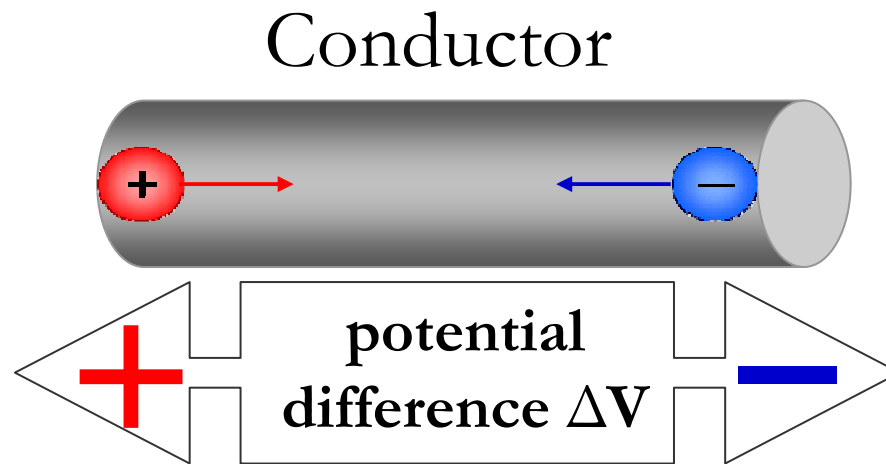


## from Electrostatic to *ElectroDynamics*



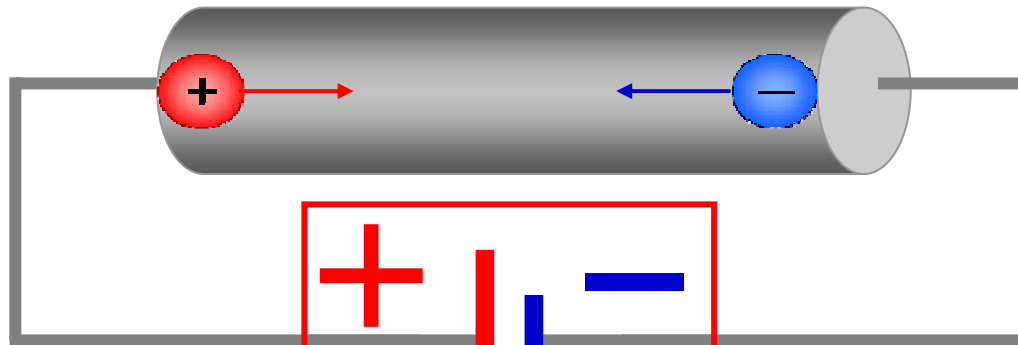
The motion of free charges of conductor balances the  
potential difference

( $\mathbf{E} = 0$  in conductor

Surface is equipotential)

To keep constant a potential difference  
what is needed ?

Conductor



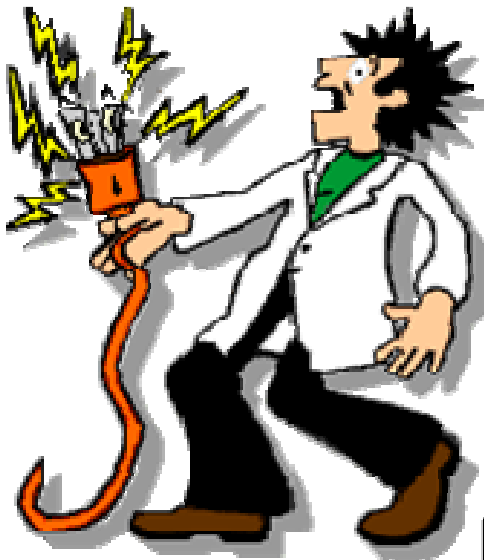
Pot. Diff. Generator



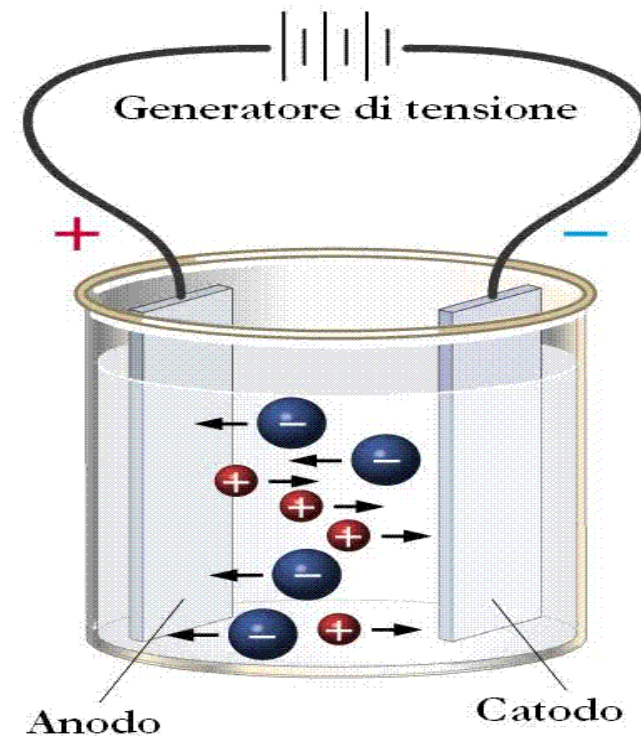
# The moving charges

## Type 1 Conductors

### Electrolytic Solutions



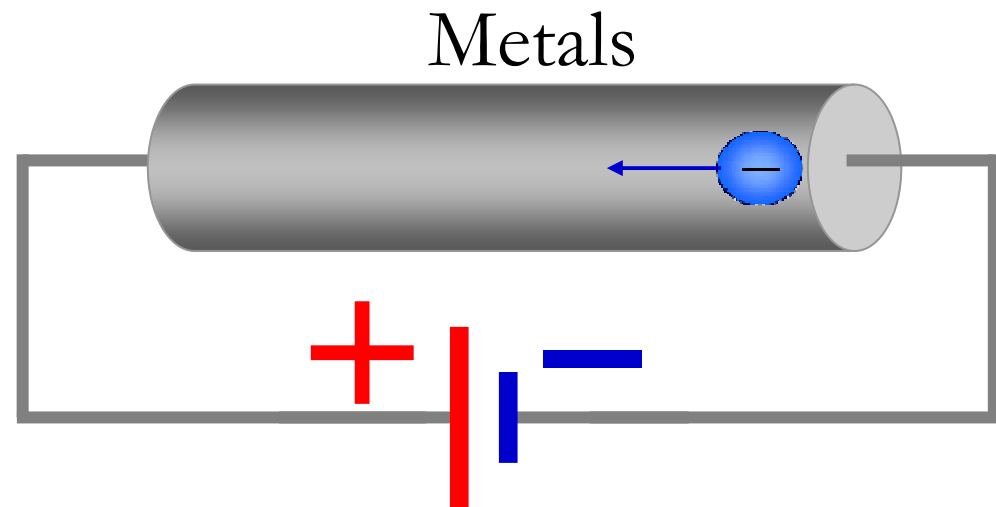
Electricity



## The moving charges in Metals

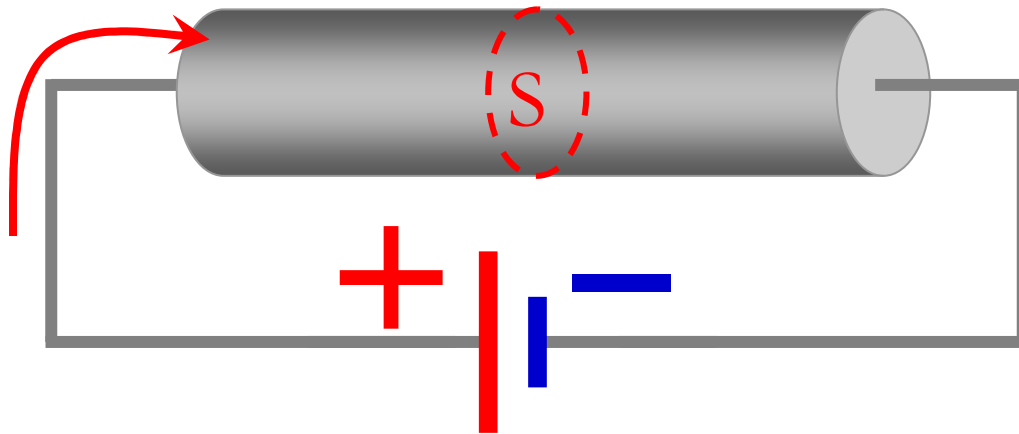
### Type 2 Conductors

Electrons are the  
charges that move



## Electric current

$I$  = quantity of charge through  $S$  in unit time



$$[I] = [Q/t] \text{ Ampere (A)}$$

$\Delta V$  can also be written  $V$

$$V = RI$$

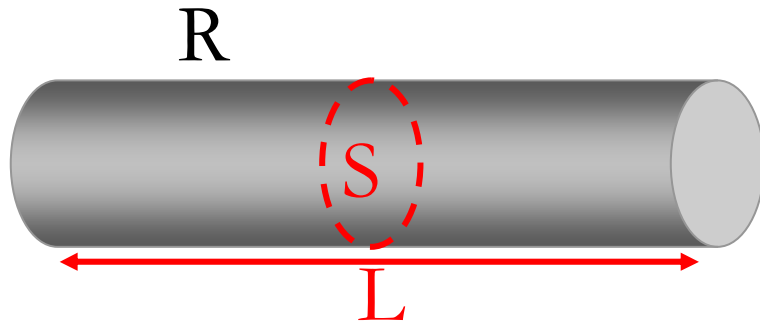
I Ohm's Law

$R$  = resistance

in  $V/A$  ohm ( $\Omega$ )

$R$  depends on type of  
conductor

## II Ohm's Law



$$R = \sigma (L/S) = (1/c)(L/S)$$

$\sigma$  = **resistivity**

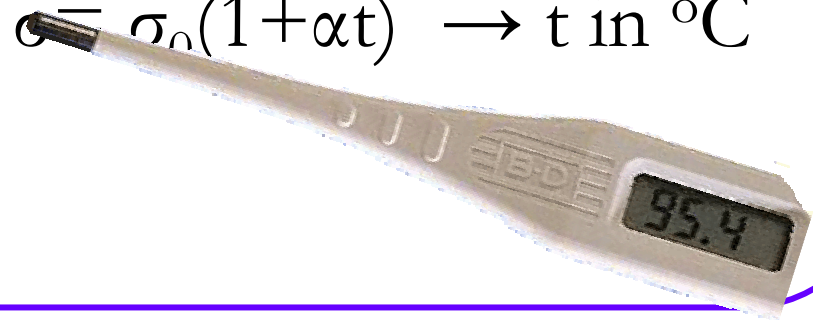
in  $\Omega \cdot m$

$c$  = **conductivity** in  $\Omega^{-1}m^{-1}$

$\sigma(\text{material}, T)$

$$\sigma = \sigma_0(1 + \alpha t) \rightarrow t \text{ in } ^\circ C$$

	$\sigma_0$ (in $\Omega m$ )	$\alpha$ (in $^\circ C^{-1}$ )
Ag	$1.6 \times 10^{-8}$	0.0038
Cu	$1.7 \times 10^{-8}$	0.0039
Au	$2.4 \times 10^{-8}$	0.0039
Al	$2.8 \times 10^{-8}$	0.0039
Fe	$10 \times 10^{-8}$	0.0050
Glass	$10^{12}$	
China	$10^{13}$	



## Esercise

A 9.00 V power supply is in a circuit made with Cu wire. The diameter is 2 mm, the temperature = 0°C, the resistance = 5.41  $\Omega$

1 Calculate the current in the circuit

$$I = V/R = 9.00/5.41 = 1.66 \text{ A}$$

2 Calculate the length of the wire

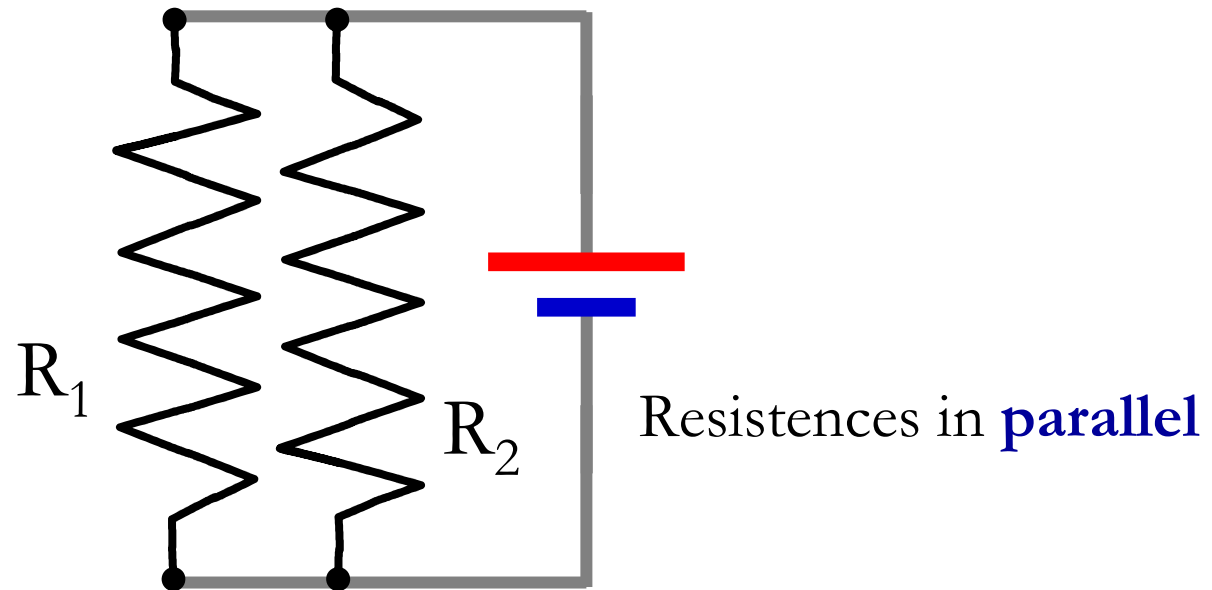
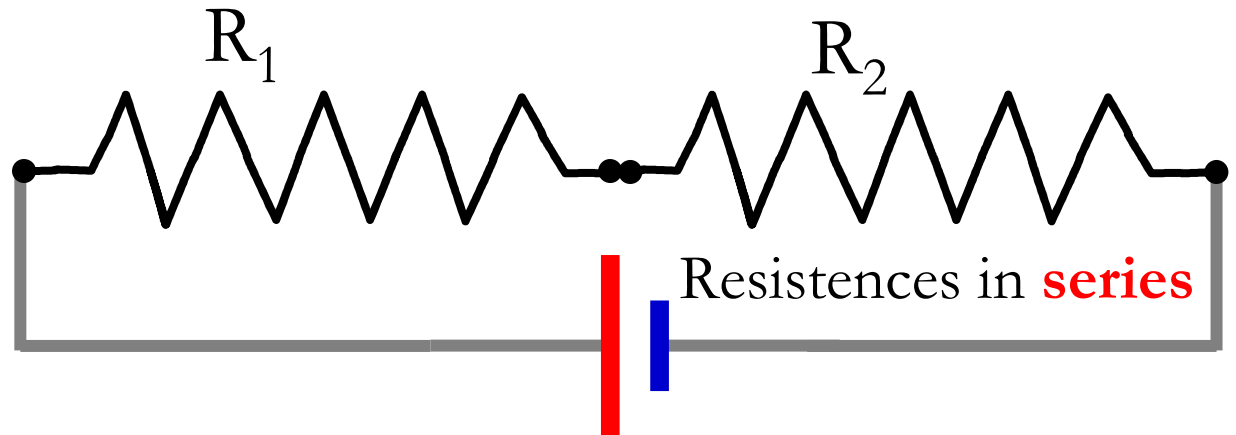
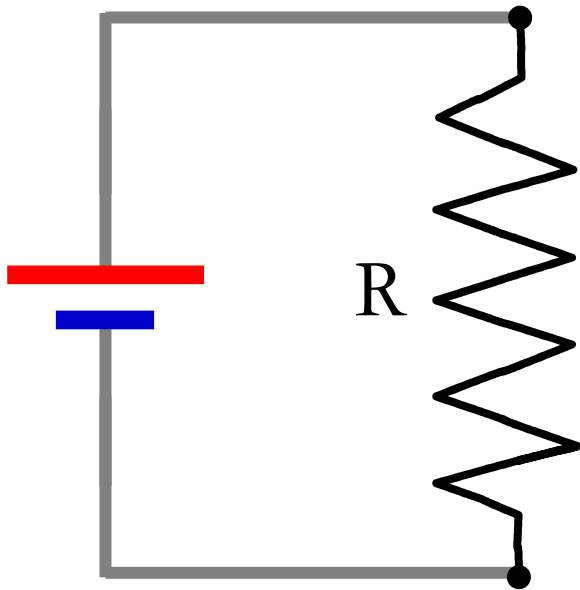
$$R = \sigma(L/S)$$

$$\sigma = \sigma_0(1 + \alpha T) \quad T=0 \rightarrow \sigma = \sigma_0 = 1.7 \times 10^{-8} \Omega\text{m}$$

$$L = RS/\sigma_0 = R\pi d^2/4\sigma_0$$

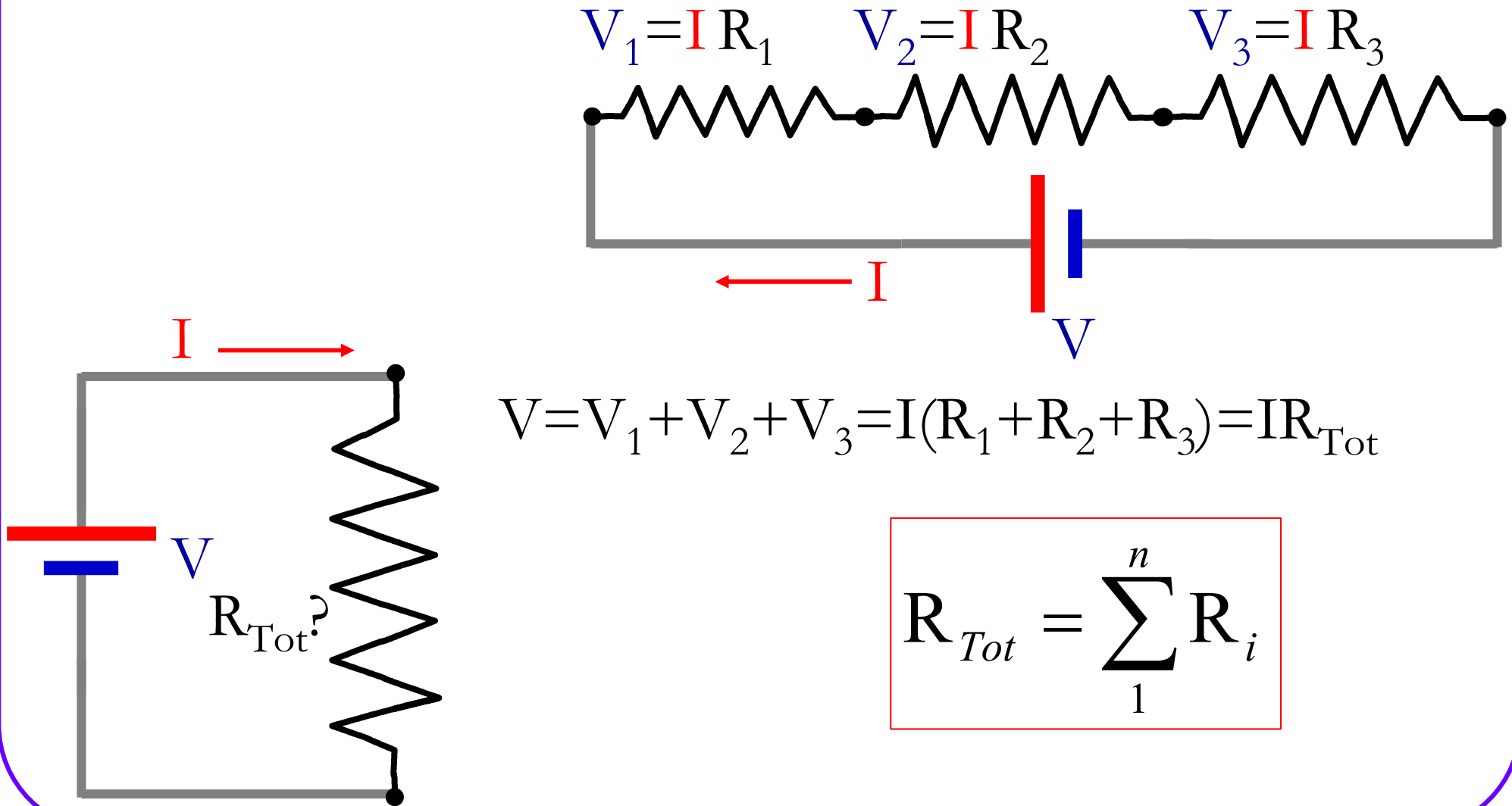
$$= 5.41 \cdot 3.14 \cdot 4 \times 10^{-6} / (4 \cdot 1.7 \times 10^{-8}) = 999 \text{ m}$$

## Representations



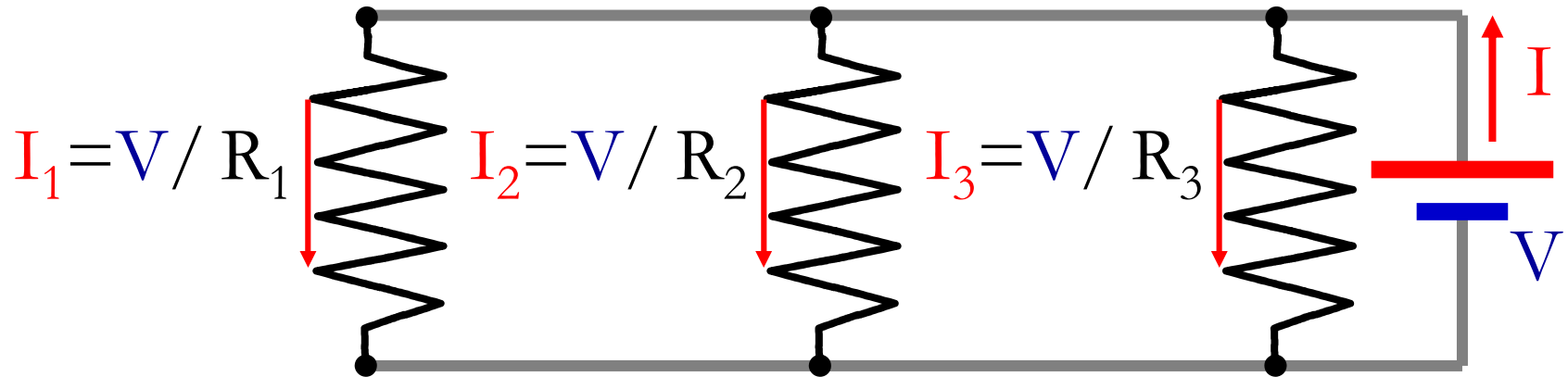


## Resistances in series



$$R_{Tot} = \sum_{i=1}^n R_i$$

## Resistances in Parallel

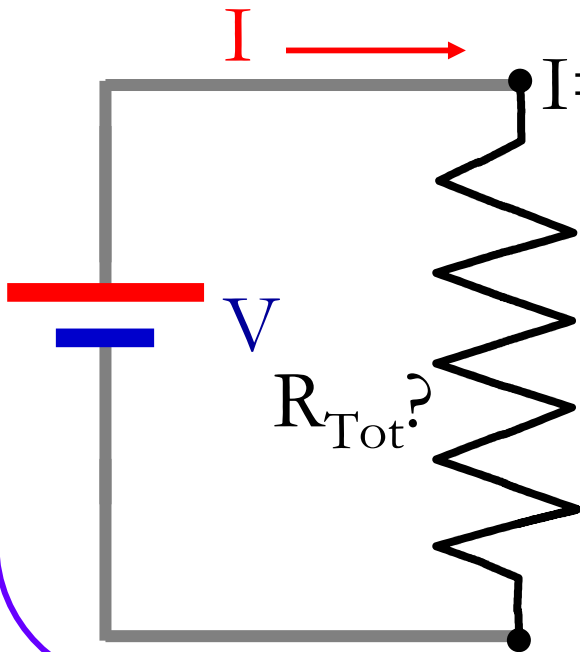


$$I_1 = V / R_1$$

$$I_2 = V / R_2$$

$$I_3 = V / R_3$$

$$I = I_1 + I_2 + I_3 = V(1/R_1 + 1/R_2 + 1/R_3) = V/R_{Tot}$$



$$R_{Tot}?$$

$$\frac{1}{R_{Tot}} = \sum_1^n \frac{1}{R_i}$$

## Esercise

A continous 60 V power supply is in a circuit with three resistences in series, 9.5 k $\Omega$ , 11.2 k $\Omega$ , 17.1 k $\Omega$ . Calculate the current

$$I = V / R_{\text{Tot}} \quad R_{\text{Tot}} = R_1 + R_2 + R_3 \quad I = V / (R_1 + R_2 + R_3)$$
$$= 60 / [(9.5 + 11.2 + 17.1) \times 10^3] = 1.57 \text{ mA}$$

**The same resistences are now in parallel. Calculate the current**

$$I = V / R_{\text{Tot}} \quad 1 / R_{\text{Tot}} = 1 / R_1 + 1 / R_2 + 1 / R_3$$
$$= [1 / 9.5 + 1 / 11.2 + 1 / 17.1] \times 10^{-3} = 0.25 \times 10^{-3} \Omega^{-1}$$

$$R_{\text{Tot}} = 4 \times 10^3 \Omega = 4 \text{ k}\Omega \quad I = 60 \cdot (0.25 \times 10^{-3}) = 15 \text{ mA}$$

## Microscopic Interpretation of Current

$n$  = number of free  $e$  per unit volume

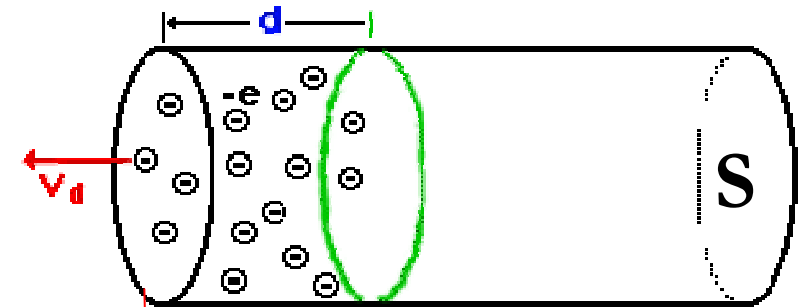
$Q = e n S d$  free charge in volume  $= d S$

$t = d/v_d$  time for  $Q$  going through  $P$

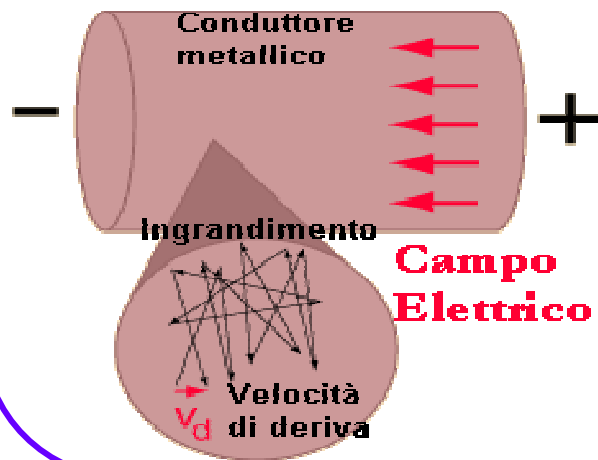
$$I = \frac{Q}{t} = \frac{enSd}{d/v_d}$$

$$I = enSv_d$$

$f_a = -k v_d$  viscous friction in a conductor



$P$  = point where  $e$  are counted



$f_e = -eE = e\Delta V/d$  electric force

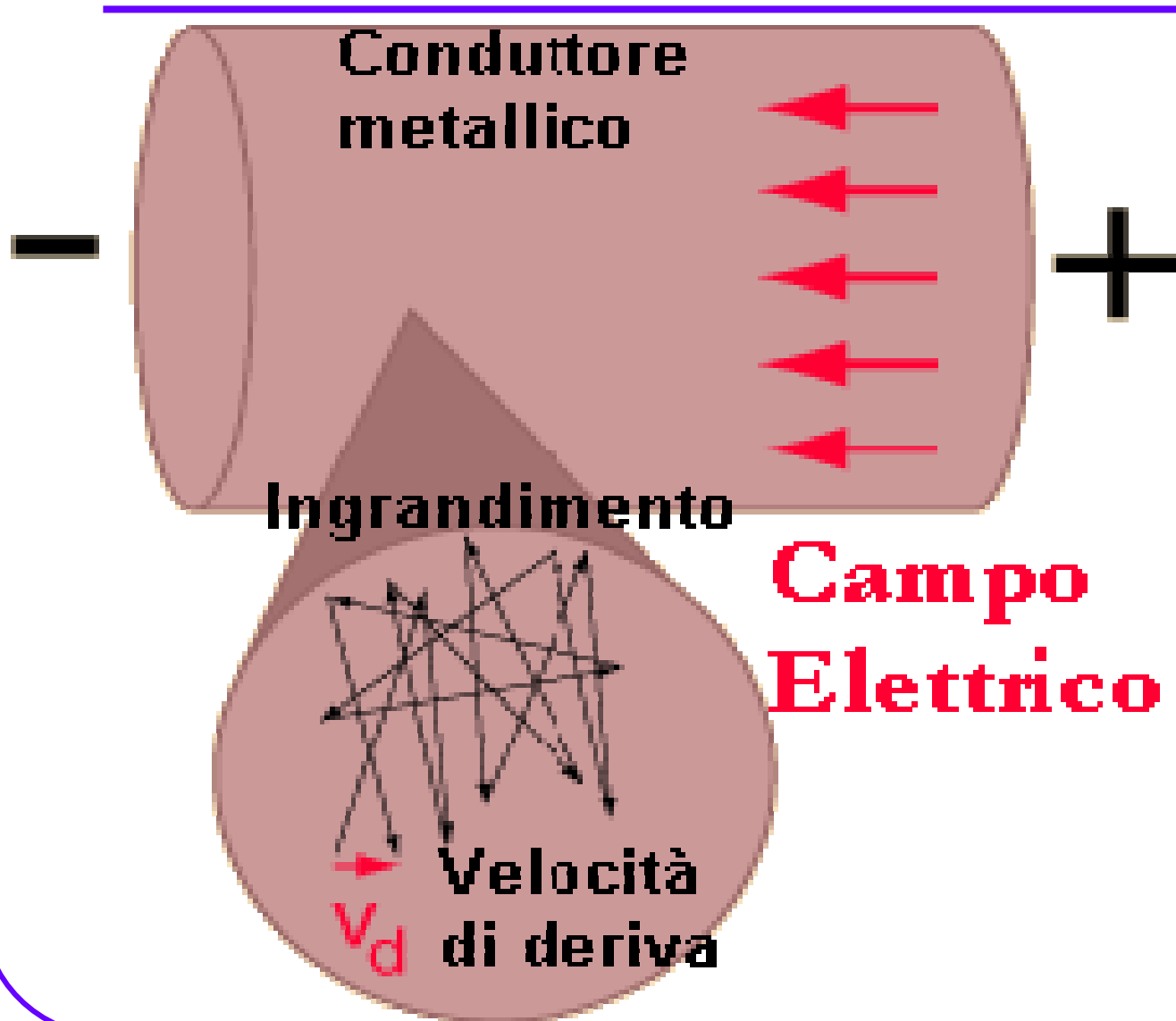
At equilibrium:  $f_e = -f_a \Rightarrow v_d = e\Delta V/(kd)$

$$I = \frac{e^2 n S}{k d} \Delta V = \frac{\Delta V}{R}$$

$$R = \frac{k d}{e^2 n S}$$

$$\sigma = \frac{k}{e^2 n}$$

## Drift velocity



## Esercise

Calculate the drift velocity in a Cu wire (1 mm diameter), when the current is = 1 A. (m. w<sub>Cu</sub>=63.5, ρ<sub>Cu</sub>=8.92×10<sup>3</sup> kg/m<sup>3</sup>)

(Assume 1 free e per atom)

$$I = enSv_d$$

$$v_d = \frac{I}{enS}$$

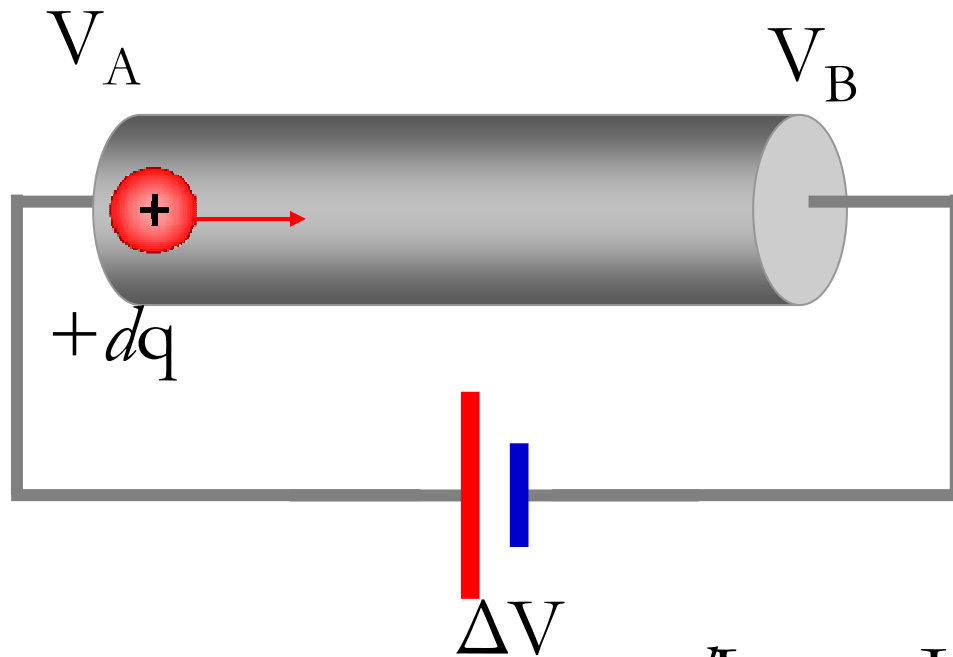
$$\begin{aligned} n &= (\text{n. of moles in unit volume}) \cdot N_A = [\rho_{\text{Cu}} / (\text{p.m}_{\text{Cu}} \times 10^{-3})] N_A \\ &= [8.92 \times 10^3 / 63.5 \times 10^{-3}] \cdot 6.02 \times 10^{23} = 8.5 \times 10^{27} \text{ m}^{-3} \end{aligned}$$

$$e = 1.6 \times 10^{-19} \text{ C} \qquad S = \pi d^2 / 4 = 3.14 \cdot (1^2) \times 10^{-6} / 4 = 7.85 \times 10^{-7}$$

$$v_d = 1 / (1.6 \times 10^{-19} \cdot 8.5 \times 10^{27} \cdot 7.85 \times 10^{-7}) = 9.4 \times 10^{-4} \text{ m/s} = 3.4 \text{ m/h}$$

## Energy Dissipated in a Conductor

Non conservative forces are acting !



$$dL_{AB} = -dq(V_B - V_A) = dq\Delta V$$

$$dq = Idt$$

$$dL_{AB} = I \Delta V dt$$

$$P = \frac{dL_{AB}}{dt} = VI = I^2 R = \frac{V^2}{R}$$

**Joule's Law**

## Esercise

---

A continuous 60 V generator is in a circuit with 3 resistances in parallel, respectively 9.5 kΩ, 11.2 kΩ, 17.1 kΩ. Calculate the power supplied by the generator

Joule's Law

$$R_{\text{Tot}} = 4 \text{ k}\Omega \quad P = V^2 / R$$

$$P = (60)^2 / 4000 = 0.9 \text{ w}$$

The same resistances are now in parallel. Calculate the power

$$P = VI = 60 \times 1.57 \text{ mA} \times \text{Volt} = 94.2 \text{ mw} = 0.0942 \text{ w}$$